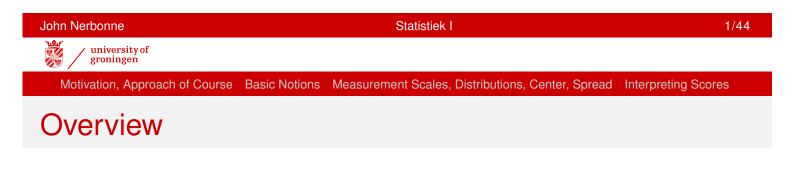


Some Descriptive Basics

John Nerbonne

CLCG, Rijksuniversiteit Groningen

www.let.rug.nl/nerbonne/teach/Statistiek-l/



- Motivation, Approach of Course
- 2 Basic Notions
- 3 Measurement Scales, Distributions, Center, Spread
 - Interpreting Scores

Statistiek I

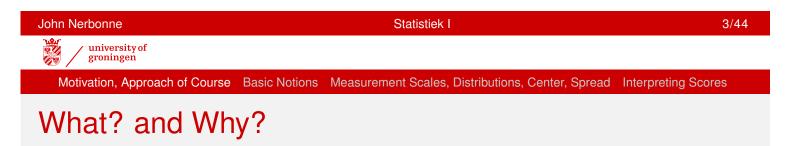
Statistiek I ATW, CIW, IK

John Nerbonne, J.Nerbonne@rug.nl, spreekuur H1311.436, ma. 16:00-16:45

Mik van Es, M. van. Es@rug.nl

Sanne Hoving, S.M. Hoving@student.rug.nl

Jet Vonk, J.M. Vonk@student.rug.nl



Statistics—collecting, ordering, analyzing data Why in general?

- Wherever studies are **empirical** (involving data collection), and where that data is **variable**.
- Most areas of applied science require statistical analysis.
- General education e.g., political, economic discussion is statistical (see newspapers).



Statistics in Language Studies

- Experiments, large empirical studies *inter alia* in communications, information science, linguistics
- Characterizing geographical, social, sexual Δ 's
- Processing uncertain input—speech, OCR, text(!)
- Evaluating intuitions (grammatical theory)
 - Bresnan article on dative shift
- Literature
 - Characteristics of authors, genres, epochs diction; sentence structure, length
 - Authorship studies (e.g. Federalist Papers)
 - Stemmata in philology (RuG diss, J.Brefeld)
- Link to cultural history, other humanities

Availability of online data increases opportunities for statistical analysis!



This course

- Practical approach
 - Emphasis on statistical reasoning
 - Understand uses (e.g. in research reports)
 - Conduct basic statistical analysis
- Look at data before and during stat. analysis
- De-emphasis on mathematics **no** prerequisite
- Use of software (SPSS)
 - Illustrates concepts, facilitates learning
 - Bridge to later use simpler
- Topics, examples from language and communications studies



- Weekly lecture (attendance required)
- Five exercises with SPSS (labs)
- Six weekly quizzes
- One exam (in het Nederlands)

Grades

• Lectures (5%)

Attendance required at all lectures. Check based on at least five (of seven) times.

• Quizzes (5%)

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- SPSS Labs (10%); Complete/Incomplete (50% if late less one week)
- Exam (80%)

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university of groningen			
Motivation, Approach of Course	Basic Notions	Measurement Scales, Distributions, Center, Spread	Interpreting Scores

Role of SPSS Labs

- "Walk through" case studies
- Think through what statistical software is demonstrating
- Acquire facility with SPSS
- Practice statistical reporting

How to approach labs

- Chance to try out ideas from lecture, book
- Ask whether your labs jibe with theory

How to waste time with labs

- Copy results from others
- Go through the motions without thinking



Descriptive vs. Inferential Statistics

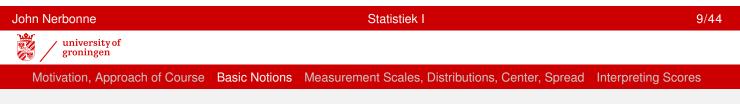
Descriptive Statistics—describe data without drawing conclusions. Example: identify average, high & low scores from a set of tests. Purpose: characterizing data more briefly, insightfully.

Inferential Statistics—describe data, likely relation to a larger set. Example: reason from sample of 1% scores to general

conclusions about all.

Purpose: learn about large **population** from study of smaller, selected **sample**, esp. where the larger population is inaccessible or impractical to study.

Note 'sample' vs. 'population.'



Variables and values

We refer to a property or a measurement as a **variable**, which can take on different **values**.

Variable	Typical Values
height	170 cm, 171 cm, 183 cm, 197 cm,
sex	male, female
reaction time	305 ms, 376.2 ms, 497 ms, 503.9 ms,
language	Dutch, English, Urdu, Khosa,
corpus frequency	0.00205, 0.00017, 0.00018,
age	19, 20, 25,

Variables tell us the the properties of **individuals** or **cases**.



Cases, variables, relations

Terminology: we speak of CASES, e.g., Joe, Sam, ... and VARIABLES, e.g. height (*h*) and native language (*I*). Then each variable has a VALUE for each case, h_j is Joe's height, and I_s is Sam's native language.

When we examine relations, we always examine the realization of two variables on each of a group of cases.

- height vs. weight on each of a group of Dutch adults
- effectiveness vs. a design feature of group of web sites, e.g. use of menus, use of frames, use of banners
- pronunciation correctness vs. syntactic category of a group of words
- phonetic vs. geographic distance on a group of pairs of Dutch towns



Tabular Presentation

Example: A test is given to students of Dutch from non-Dutch	
countries. Variables:	

Variable	Values							
area of origin	EUrope, A	Merica	i, AFrica	ASia				
test score	0-40							
Sex	Male, Ferr	nale						
		area	score	sex				
		EU	22	Μ				
Here is part of the results.		AM	21	F				
		÷	÷	:				
Three variables,	where sco	re is nu	umeric &	each rov	w CASI			

Tables show *all* data, but large tables are not insightful.

SPSS Coding

It is often advantageous to code information in a particular way for a particular software package.

In general, SPSS allows fewer manipulations and analyses for data coded in letters. Use numbers as a matter of course. This causes us to recode 'area of origin' and 'sex', since these were coded in letters.

area of origin	EUrope	AMerica	AFrica	ASia
	0	1	2	3
sex	Male	Female		
	1	2		

Notate bene: this is a weakness in SPSS. In general, it is good practice to use meaningful codings. But in SPSS, this will limit what you can do—use numbers!



Classifying

It is also sometimes useful to group numeric values into classes. We might group scores into 0-16 (beginner), 17-24 (advanced beginner), 25-32 (intermediate), and 33-40 (advanced).

area	score	sex	score class
0	22	1	1
1	21	2	1
2	15	2	0
3	26	1	2
:	:	:	
•	•	•	

Grouping numerical information into classes loses information. Care!

Reminder:

area of origin	EUrope	AMerica	AFrica	ASia
	0	1	2	3
sex	Male 1	Female 2		

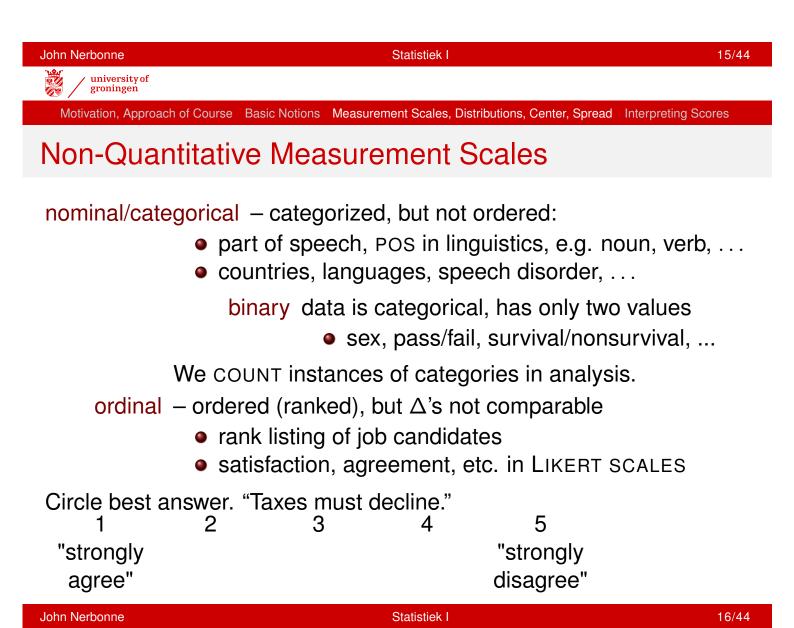
Data/Measurement Scales

nl. *meetniveau*

categorical scales nominal, ordinal quantitative scales interval, ratio, etc.

Scale determines type of statistics possible, e.g. mean (average).

We can average quantitative data, but not categorical data. We speak of the average height of an individual (quantitative), but not his average native language (categorical).

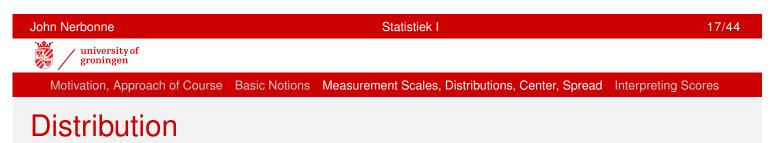




Quantitative/Numerical Scales

- interval ordered, Δ's comparable, but no true zero (needed for multiplication)
 temperature (in Celsius of Fahrenheit)
 ratio like interval *plus* zero available
 height, weight, age
 elapsed time, reaction time
 "logarithmic" like ratio, but successive intervals multiply in size
 Richter scale in earthquakes
 loudness, pitch (auditory perception)
 - improvement (in error) rates (often)

Log. scales often result from TRANSFORMATIONS applied to data.



We are often interested not in a particular value of a variable for a particular invidual, but rather all the values of the variable and how often they occur.

The DISTRIBUTION of a variable shows its values and how often they occur.

The CENTER and SPREAD refer to the variable's distribution.



Visualizing Distributions

DISTRIBUTION is the pattern of variation of a variable Example: Number of health web-site visitors for 57 consecutive days.

279	244	318	262		321	165	180	201	252
145	192	217	179	182	210	271	302	169	192
156	181	156	125	166	248	198	220	134	189
141	142	211	196	169	237	136	203	184	224
178	279	201	173	252	149	229	300	217	203
148	220	175	188	160	176	128			

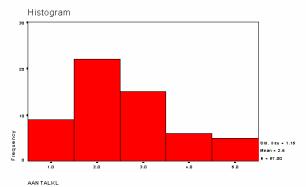
stem 'n leaf diagram sorts by most significant (leftmost) digit. As above, ignoring rightmost digit.

- 1 | 223344444556666667777788888889999
- 2 | 000011112222344556777
- 3 | 00123



Displaying Distributions via Histograms

Histograms show how frequently all values appear, often require categorization into small number of ranges (\leq 10).



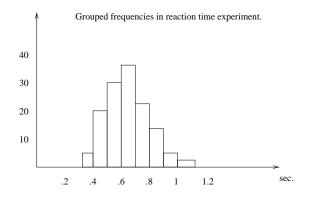
Look for general pattern, outliers, symmetry/skewness.



Distributions of Quantitative Variables

Most **quantitative variables** take any number of values. Variables that take more than about 7 values are often analysed as quantitative e.g., test scores. We often display their frequency distributions by **grouping** values.

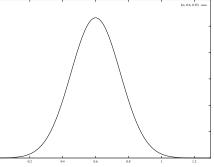
Example: histogram of reaction times.





Density Curves

Smoothed curves also plot area proportional to relative frequency. Same reaction time data:



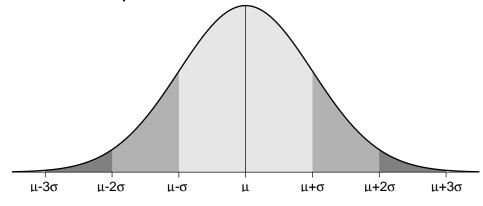
Most very close to 0.6 sec (600ms) \neg interpret as 'p% of reaction times = 600ms.' 700ms reaction time ~ 25% —maybe **no** reaction time was exactly 600ms

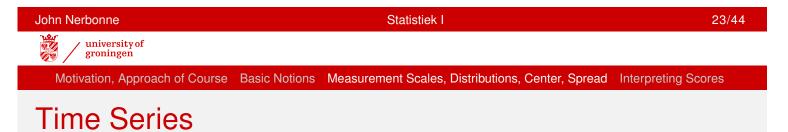


Probability Density Curves

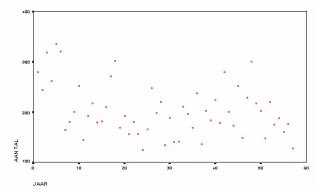
- assign (fractional) values to events, 0 ≤ P(e) ≤ 1, where an event is a collection of (possible) occurences
- sum to one (all possible events) $\int_{-\infty}^{\infty} P(x) dx = 1$

lots of possibilities, most famously "normal" distributions—"bell-shaped" curve





Same variable at regular intervals e.g., indices, web site visits, ...



Change often focus of attention



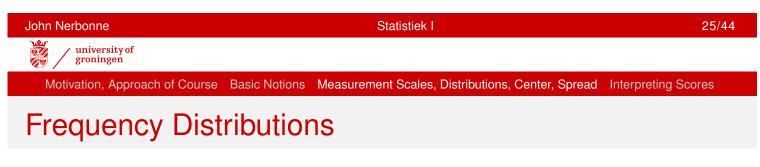
Frequency Distributions

Frequency distributions (frequentieverdelingen) show how often various values occur.

absolute frequency How many times values are seen, e.g., 16 men, 24 women

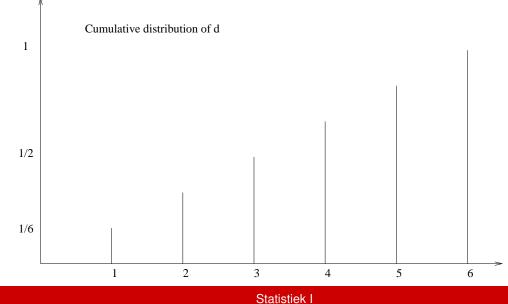
relative frequency What percentage or fraction of all occurrences, e.g., 40% (= 16/40) men, 60% (= 24/40) women

> Example: relative frequency of an honest die (flat graph, with each rel. frequency $\approx 1/6$)



cumulative frequency how often values at least as large as a given value occur.

Example: cumulative relative frequency of an honest die.



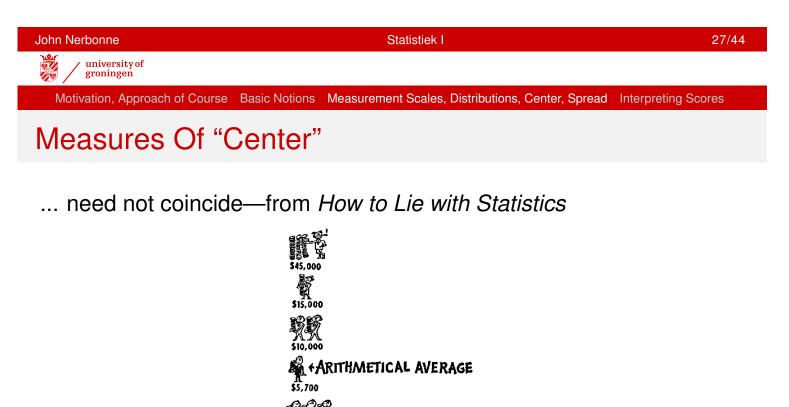


Central Tendency

- mode most frequent element the only meaningful measure for nominal data
 median half of cases are above, half below the median available for ordinal data.
 - mean arithmetic average

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$$
$$\frac{1}{n} \sum_{i=1}^n x_i$$

 μ for populations, *m* (and \bar{x}) for samples



+ MEDIAN (the one in the middle.) 12 above him, 12 below

\$3,000



Special—Moving Averages

Some measures fluctuate due to weather, business cycles, chance

moving average sums over overlapping intervals to eliminate some effects of fluctuation

Year	Export	5-yr Ave.	6-yr. Ave
1855	95.7		
1856	115.8		
1857	122.0	116.1	
1858	116.6	124.1	121.8
1859	130.4	126.0	125.0
1860	135.9	126.4	127.7
1861	125.1	132.4	133.4
1862	124.0	138.4	140.0
1863	146.5	144.4	
1864	160.4		
1865	165.8		

from J.T.Lindblad Statistiek voor Historici



x-ile's

Quartiles, quintiles, percentiles-divide a set of scores into equal-sized groups

	37	68	78	90
	49	71	79	90
	54	71	79	90
quartiles:	56	73	83	92
quai inco.	60	75	83	94
	64	76	85	95
	65	77	87	96
	65	77	88	97

 q_1 1st quartile—-dividing pt between 1st & 2nd groups; q_2 —div. pt. 2nd & 3rd (= median!)

percentiles: divide into 100 groups—thus $q_1 = 25$ th percentile, median = 50th, ...

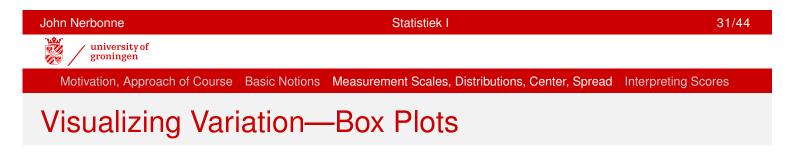
Score at *n*th percentile is better than *n*% of scores.

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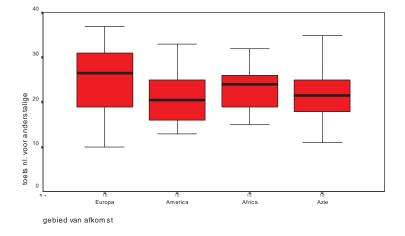


Measures of Spread/Variation

- none for nonnumeric data! why?
- minimum, maximum lowest, highest values
- range difference between minimum and maximum
- interquartile range $(q_3 q_1)$ —center where half of all scores lie
- semi-interquartile range $(q_3 q_1)/2$
- "box-n-whiskers" diagrams showing q₂ & q₃, range, median



"box-n-whiskers" plot w. q_2 , q_3 , range, median



Results "Dutch for Foreigners" for four groups of students.

"Boxes" show $q_3 - q_1$, line is median. "Whiskers" show first and last quartiles.



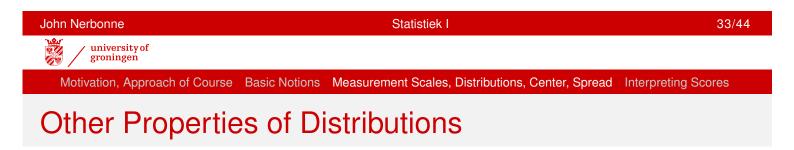
Spread of Quantitative Variables

deviation is difference between observation and mean variance average square of deviation

$$\sigma^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

standard deviation square root of variance $\sigma = \sqrt{\sigma^2}$ σ^2 for population, s^2 for sample

—square allows orthogonal sources of deviation (error) to be analyzed $e^2 = e_1^2 + e_2^2 + \cdots + e_n^2$



skew "scheefheid" measure of balance of distribution

$$= \left\{ \begin{array}{ll} - & \text{if more on left of mean} \\ 0 & \text{if balanced} \\ + & \text{if more on right} \end{array} \right.$$

kurtosis relative flatness/peakedness in distribution

$$= \begin{cases} - & \text{if relatively flat} \\ 0 & \text{if as expected} \\ + & \text{if peak is relatively sharp} \end{cases}$$

-seen in SPSS, not used further in this course



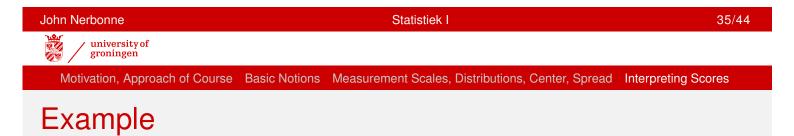
Standardized Scores

"Tom got 112, and Sam only got 105"

-What do scores mean?

Knowing μ , σ one can **transform** raw scores into **standardized scores**, aka **z-scores**:

$$z = \frac{x - \mu}{\sigma} = \frac{\text{deviation}}{\text{standard deviation}}$$



Suppose $\mu = 108$, $\sigma = 10$, then

$$z_{112} = \frac{112 - 108}{10} \qquad 0.4$$

$$z_{105} = \frac{105 - 108}{10} \quad -0.3$$

z shows distance from mean in number of standard deviations.



Standardized Variables' Distributions

If we transform **all** raw scores into **z-scores** using:

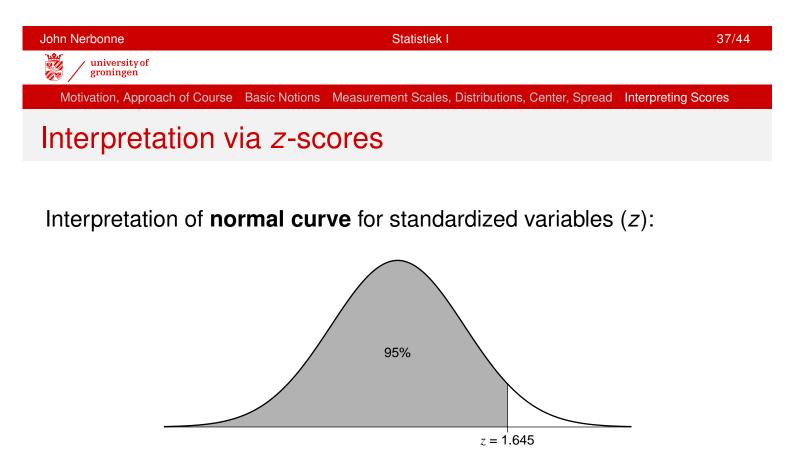
$$z = \frac{x - \mu}{\sigma} = \frac{\text{deviation}}{\text{standard deviation}}$$

We obtain a **new** variable <u>z</u>, whose

mean is 0 standard deviation is 1

z-score = distance from μ in σ 's

uses: interpretation, sampling, hypothesis testing



In every normal curve, 95% of the mass is under the curve below the point which is 1.645 standard deviations above the mean.



Normal Curve Tables (based on z-scores)

See M&M, Tabel A, pp.696-97

Z	.00	.01	.02	.03	.04	.05	.06	
•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	• • •
•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•

where z is the standardized variable:

$$z = \frac{x - \mu}{\sigma} = \frac{\text{deviation}}{\text{standard deviation}}$$



Interpretation via z-scores

If distribution is normal, then standardized scores correspond to percentiles

Z	.00	.01	.02	.03	.04	.05	.06	
		-						•
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	
•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	-

Table specifies the correspondence $(\div 100)$, containing the fraction of the frequency distribution less than the specified *z* value. Tables in other books give, e.g., $1 - (Percentile \div 100)$.



Interpretation via *z*-scores

Typical questions, where tables can be applied

- $P(\underline{z} > 1.5) = ?$ —What's the chance of a *z* value greater than 1.5?
- $P(\underline{z} \le 1.5) = ?$

•
$$P(\underline{z} \leq -1.5) = ?$$

• $P(-1 \leq \underline{z} \leq 1) = ?$

We assume normally distributed variables. Exercises: "Interpretation of Normal Distribution"



Checking Normality Assumption

Some statistical techniques can only be applied if the data is (roughly) normally distributed, e.g., *t*-tests, ANOVA.

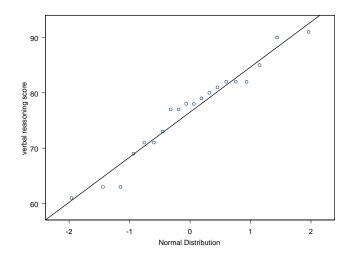
How can one check whether the data is normally distributed? **Normal Quantile Plots** show (roughly) straight lines if data is (roughly) normal.

- Sort data from smallest to largest—showing its organisation into quantiles
- Calculate the *z*-value that would be appropriate for the quantile value (normal-quantile value), e.g., z = 0 for 50th percentile, z = -1 for 16th, z = 2 for 97.5th, etc.
- Plot data values against normal-quantile values.

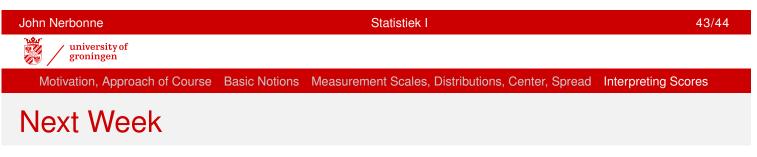


Normal Quantile Plots

Example: Verbal reasoning scores of 20 children



Plot expected normal distribution quantiles (x axis) against quantiles in samples. If distribution is normal, the line is roughly straight. Here: distribution roughly normal.



Samples, Sample Means