Statistiek I
Choice of Statistical Tests

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http://www.let.rug.nl/nerbonne/teach/Statistiek-I/

Choice of Statistical Tests

Nonparametric Fallbacks

non-numeric — numeric

χ^2

1 variable — relations

compare ave. — **Correlation** (Pearsons r) ⟶ **Spearman's ρ**

σ known — σ unknown

z-test

2 grp — ≥ 3 grp

t-test — **ANOVA** ⟶ **Kruskal-Wallis**

different subjects — same subjects

paired t-test ⟶ **Wilcoxon**

t-test unrelated samples ⟶ **Mann-Whitney U-Test**
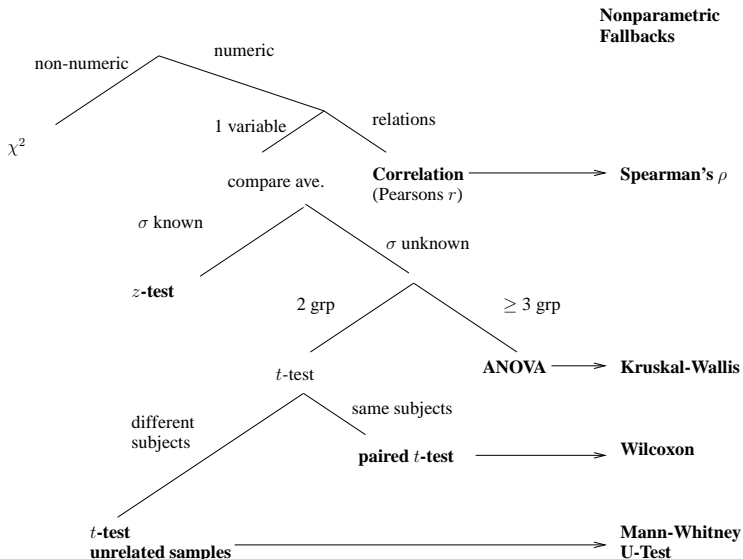
Choice of Statistical Tests

Nominal Data

- χ^2 test of independence
    - check whether one variable influences another
    - organize one set of variable values into columns, the second into rows
    - (reformulated) question: is the distribution roughly the same in the different rows?
    - H_0: no influence

	Pet Ownership		
Owner	**Type of Pet**		
	dogs	cats	other
boys	39	55	6
girls	26	65	9

- no cell with expectation of zero's
- small 2 × 2 tables require *Yates* correction
- to measure effect size, user Cramér's V
- for paired data, McNemar's test

Nominal Data

Sign Test

- can be used, e.g.,
    a. to test agreement in judgement
    b. to indicate improvement
- interpretation
    a. $+$ indicates agreement, $-$ disagreement
    b. $+$ indicates improvement, $-$ none
- question: is the breakdown of $+$'s and $-$'s a chance breakdown?
- relatively insensitive
- almost always applicable (even when original data in not normally distributed, and even asymmetrical)

Means

To check for a difference in means (averages) where the standard deviation is known, the most sensitive test is the *z*-test.

- how many standard errors separate the two sample averages?

$$z = \frac{m_1 - m_2}{\sigma/\sqrt{n_1 + n_2}}$$

- averages are always normally distributed (no need to check for normality
- H_0: no difference in averages
- interpret using standard-normal tables

To express effect size whenever comparing means, characterize difference in terms of standard deviations.

Averages, σ unknown

To check for a difference in averages where the standard deviation is unknown, first ask whether are testing two different groups (unrelated samples), or two scores from one group (paired data).

t-test for unrelated samples

- t statistic like z, uses s instead of σ
- H_0: no difference in averages
- sample size is important
    - if $n \leq 15$, dist. must be normal
    - if $n \geq 40$, z is almost identical
- if t cannot be used, try **Mann-Whitney U test**
- with 3 or more groups, use **ANOVA**

Mann-Whitney U-Test

alternative to *t*-test (unpaired data)

- H_0 : samples from same population
- often applied to Likkert scale data
- **generalization** to several groups: **Kruskal-Wallis**

Averages, σ unknown

To check for a difference in averages where the standard deviation is unknown and two scores from one group (paired data).

t-test for paired data

- uses same t statistic as t-test for unrelated samples, uses s instead of σ
- H_0: no difference in averages
- sample size is important
  - if $n \leq 15$, dist. must be normal
  - if $n \geq 40$, z is almost identical
- if t cannot be used, try **Wilcoxon test**

Wilcoxon

Wilcoxon's Signed Rank Test

- also applicable to ordinal data
- fallback for paired *t*-test
- distribution should be roughly symmetric, not skewed
- if data asymmetric, try **sign test**

Next Week—Exam

Break a leg!