



STATISTICAL ANALYSIS

Repeated Measures
and (M)ANOVA designs



Why repeated measures?

- What is the greatest source of variance in a (psycholinguistic response time) experiment?



Why repeated measures?

- What is the greatest source of variance in an experiment?
 - people



Between Subjects Effects

last table of Repeated measures

Tests of Between-Subjects Effects

Measure: MEASURE_1

Transformed Variable: Average

Source	Type III Sum of Squares	df	Mean Square	F	Sig.
Intercept	85863235,4	1	85863235,42	683,157	,000
Error	4399009,151	35	125685,976		



Why repeated measures?

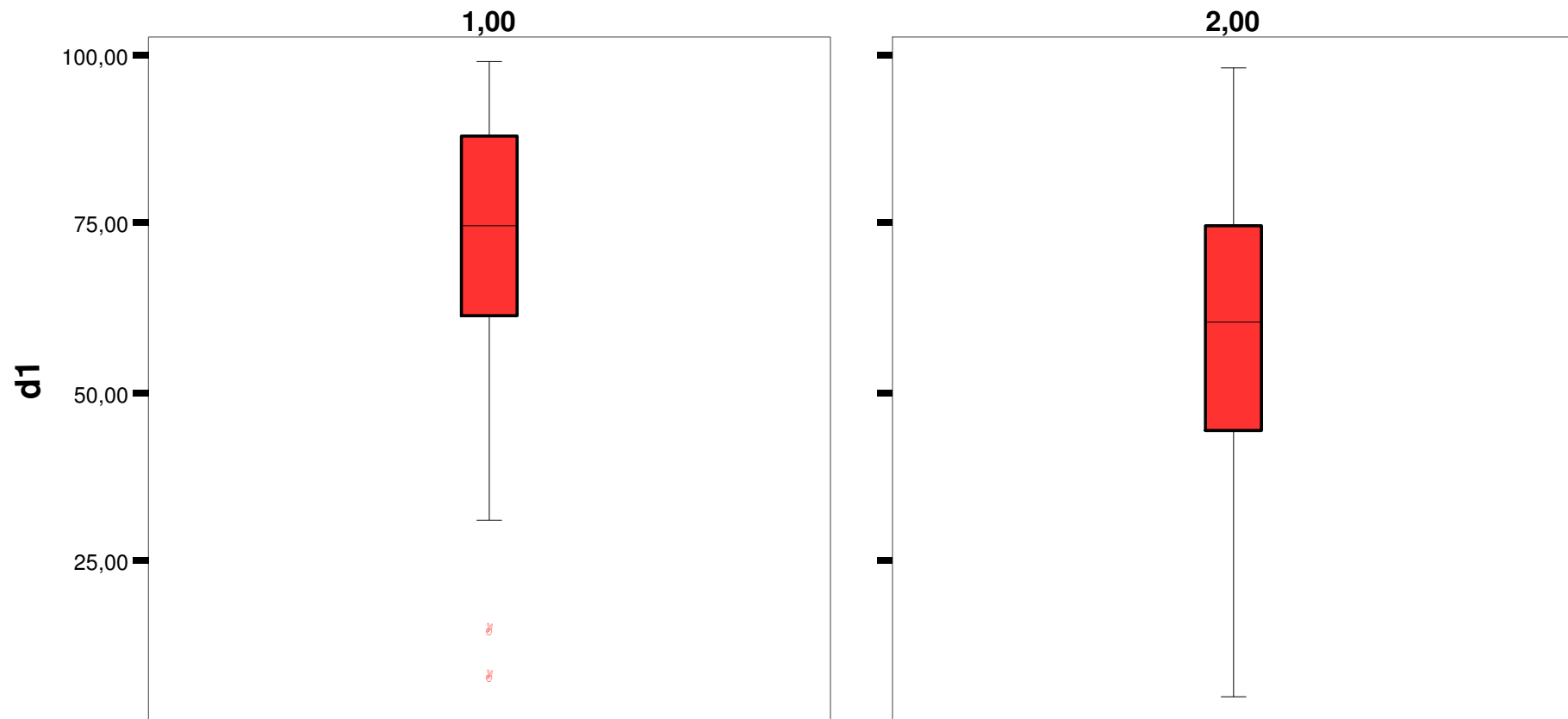
- What is the greatest source of variance in an experiment?
 - People
 - Can we get rid of this noise?
 - Repeated measures designs



Why Repeated Measures?

- Concrete example

Are these distributions (conditions) really different?

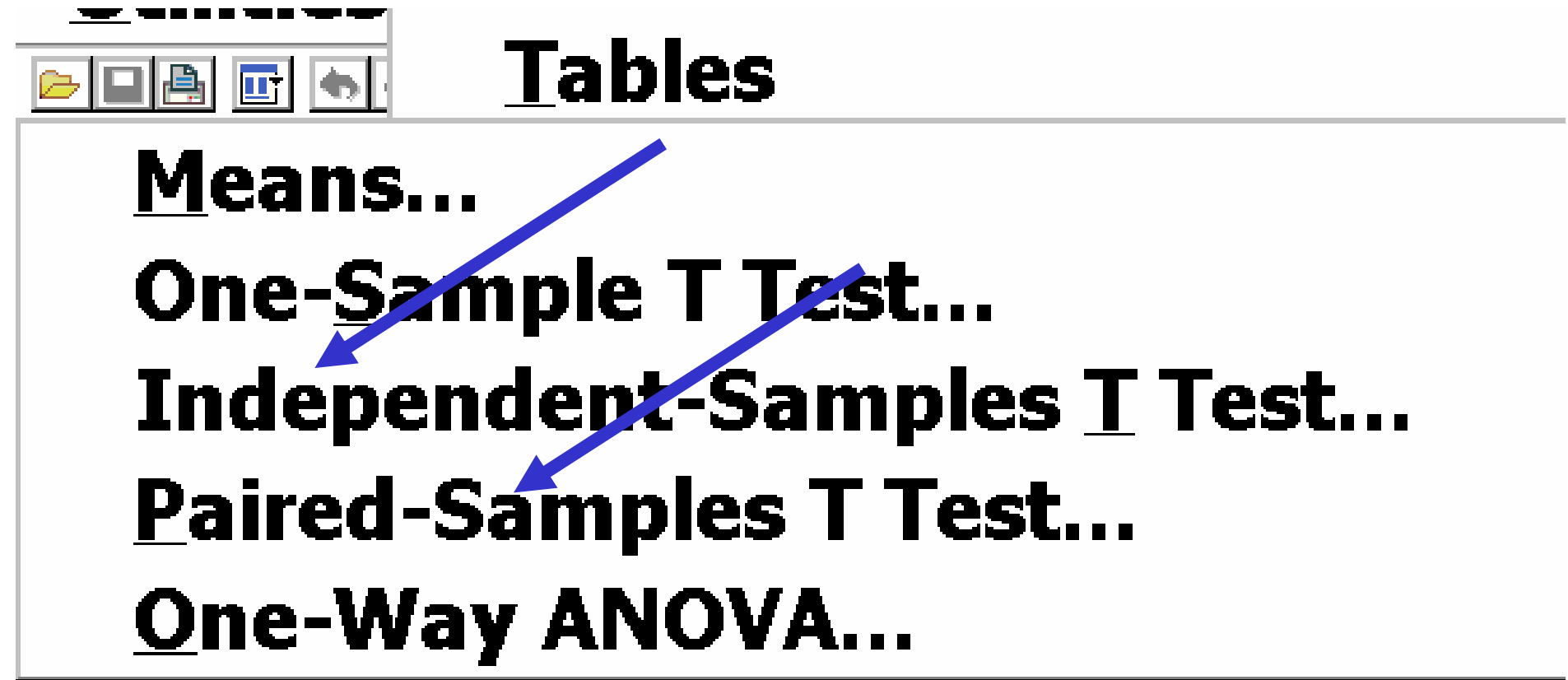




Can we use a t-test?

- Equivalent standard deviations?

Independent Samples vs. Paired Samples



Tables

- Means...**
- One-Sample T Test...**
- Independent-Samples T Test...**
- Paired-Samples T Test...**
- One-Way ANOVA...**



Independent Samples

Independent Samples

		Levene's Test for Equality of Variances				
		F	Sig.	t	df	Sig.
d1	Equal variances assumed	,098	,757	,771	30	
	Equal variances not assumed			,771	29,422	



Independent Samples

Independent Samples Test

t-test for Equality of Means						
df	Sig. (2-tailed)	Mean Difference	Std. Error Difference	95% Confidence Interval of the Difference		
				Lower	Upper	
30	,447	7,06250	9,16559	-11,65614	25,78114	
29,422	,447	7,06250	9,16559	-11,67157	25,79657	



Paired Samples (1)

Paired S

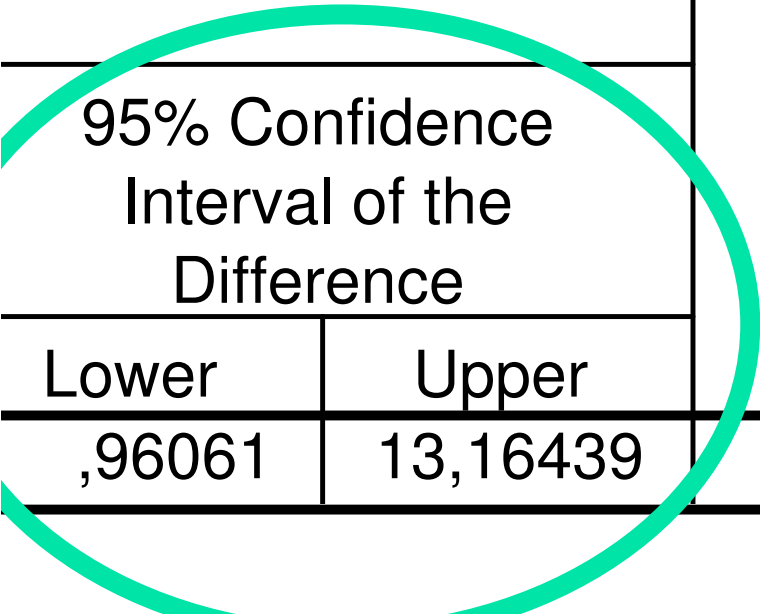
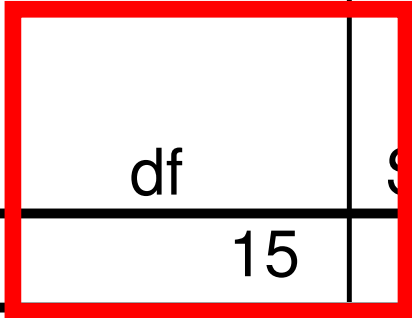
		Paired Differences		
		Mean	Std. Deviation	Std. Error Mean
Pair 1	d1 - d2	7,06250	11,45116	2,86279



Paired Samples (1)

mples Test

95% Confidence Interval of the Difference				
Lower	Upper	t	df	Sig. (2-tailed)
,96061	13,16439	2,467	15	,026



Paired Samples (2)

Paired Sample

		Paired Differences			
		Mean	Std. Deviation	Std. Error Mean	95% Lower Bound
Pair 1	d1 - d2	7,06250	50,51134	12,62784	-19,84

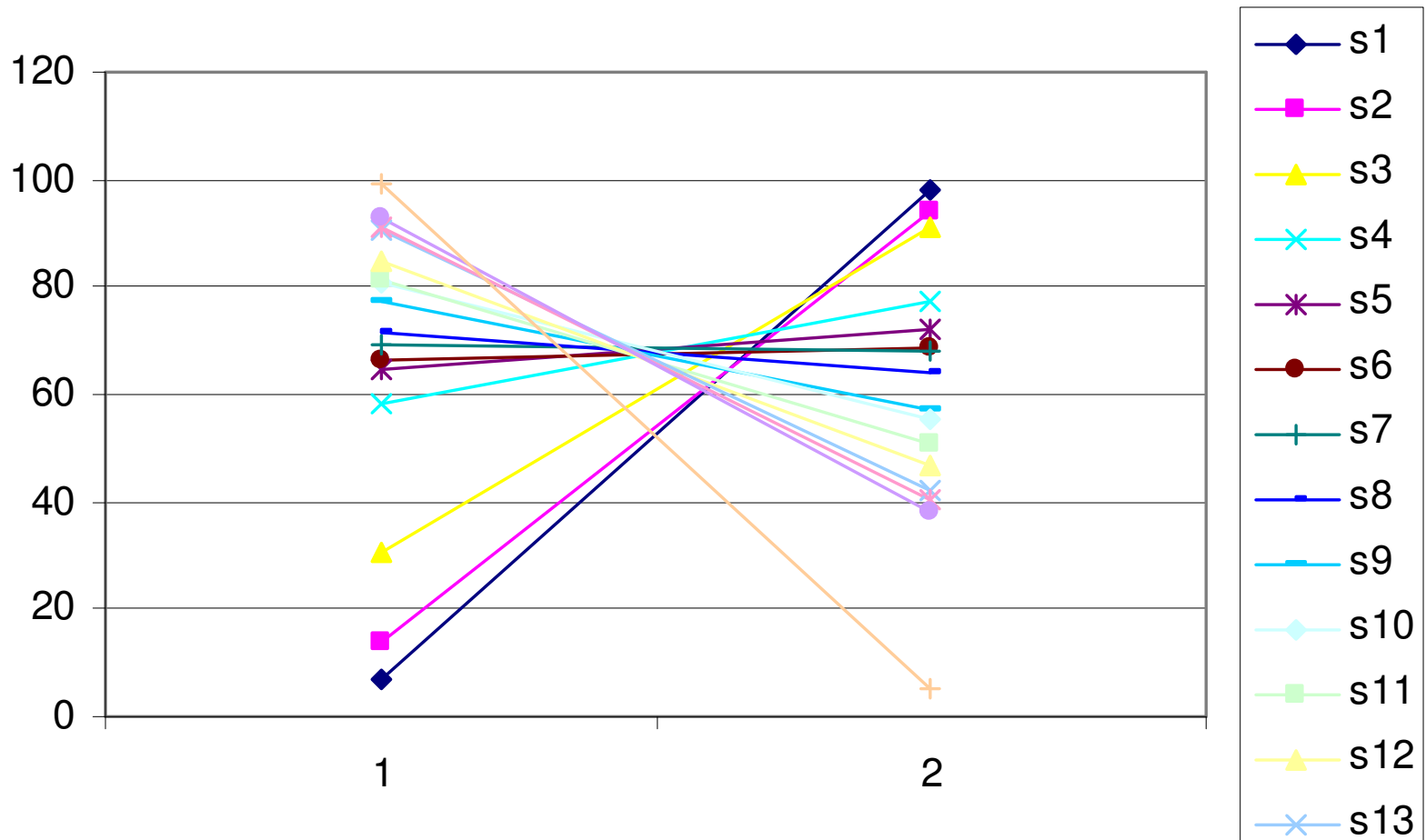


Paired Samples (2)

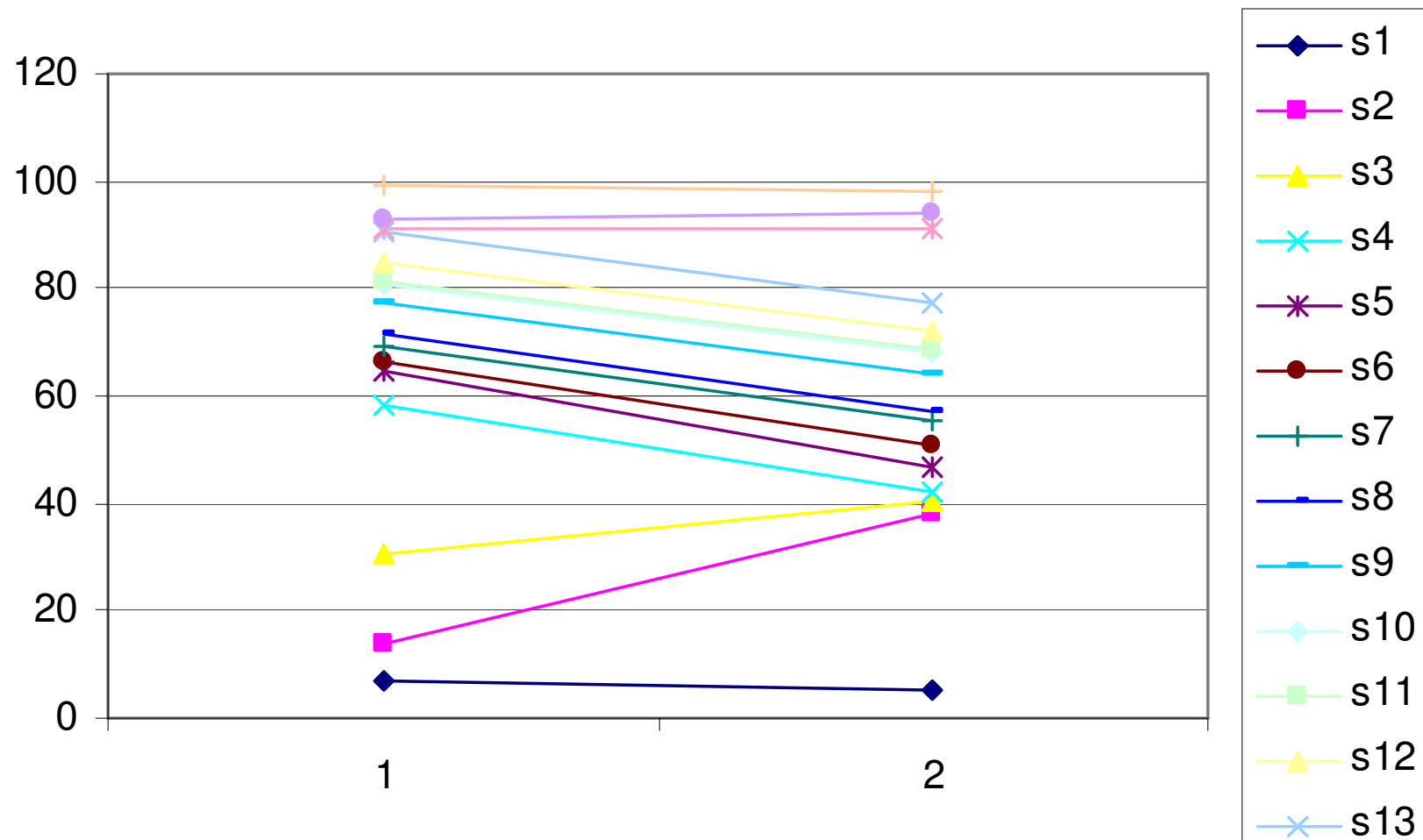
Samples Test

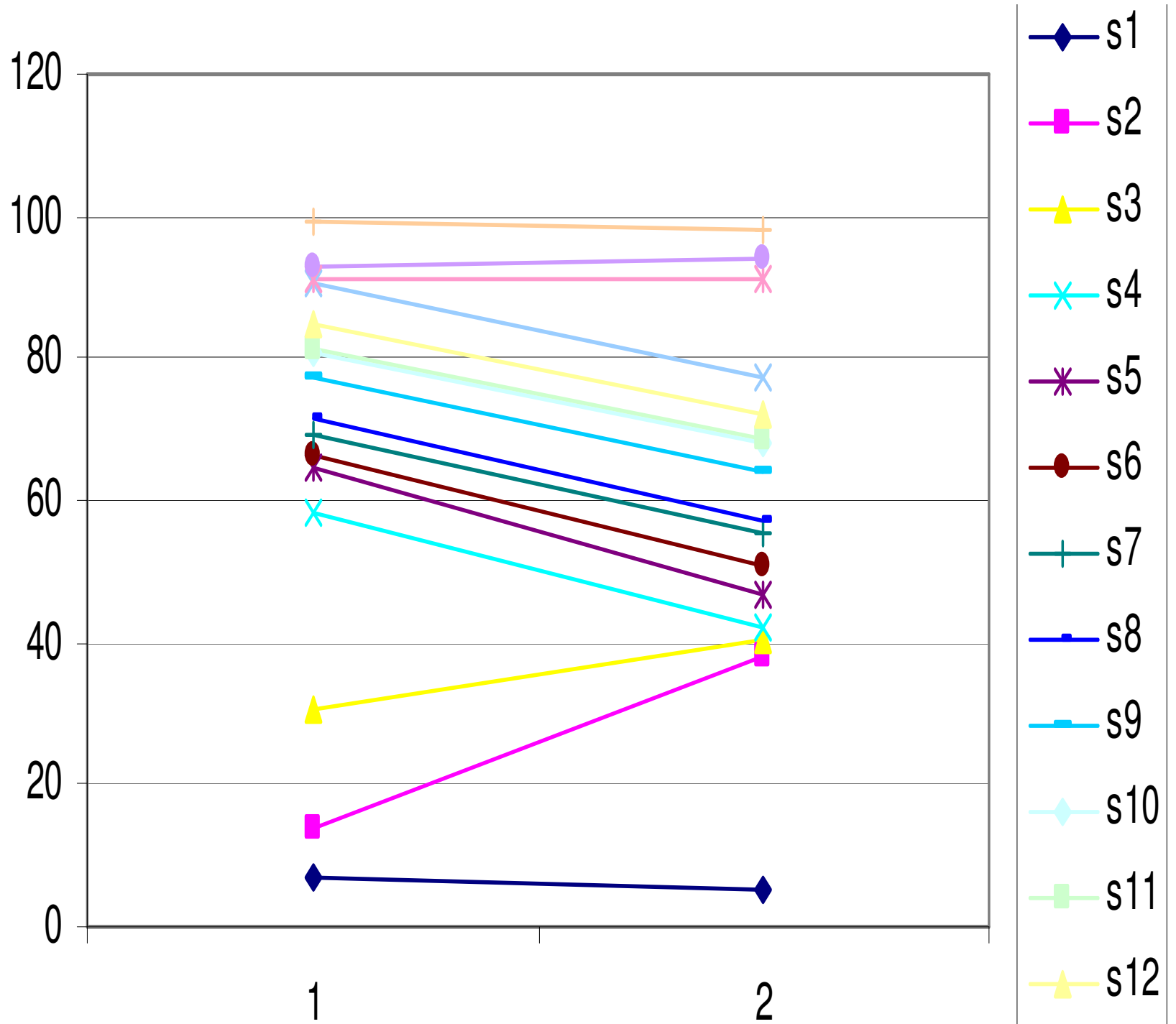
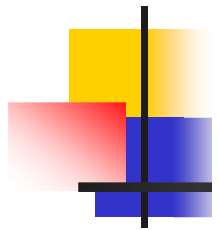
95% Confidence Interval of the Difference		t	df	Sig. (2-tailed)
Lower	Upper	,559	15	,584
-19,85310	33,97810			

Why? Consistency



Why? Consistency







Repeated Measures

- Example with large between subject variability
- small effect size
- Here within subject (repeated measures) design is usually invaluable



Repeated Measures

- Is a spurious effect possible using between group design when this is not the correct design?
- Yes, if there is sufficient accidental clustering of responses in one condition
 - Due to inflated degrees of freedom
 - Even though these are not consistent



Repeated Measures

- Unless you are specifically interested in intersubject variability
- Always use repeated measures where possible



ANOVA vs. T-test

- In some experiments we have more than two levels of a factor
- So paired samples don't work too well
- Why not?



Experiment with three levels

- Sentences containing ambiguous words
- Sentence completion test
 - Context supporting more frequent (dominant) meaning
 - Context supporting less frequent (subordinate) meaning
 - Context equally consistent with each



Experiment with three levels

- Het akkoord kon met weinig moeite worden ____
- Het akkoord kon door de politici worden ____
- Het akkoord kon door de pianist worden ____



Experiment with three levels

- Is there an effect of context?
- To increase completions indicating that the subordinate meaning has been selected
- To increase completions suggesting the ***dominant*** meaning has been selected?



ANOVA vs. T-test

- Carry out two t-tests (dominant and subordinate context relative to neutral)?
- Or an ANOVA looking for differences across all three levels?



Probability

Test

Confidence interval of the difference		t	df	Sig. (2-tailed)
	Upper			
01	13,16439	2,467	15	,026



Probability

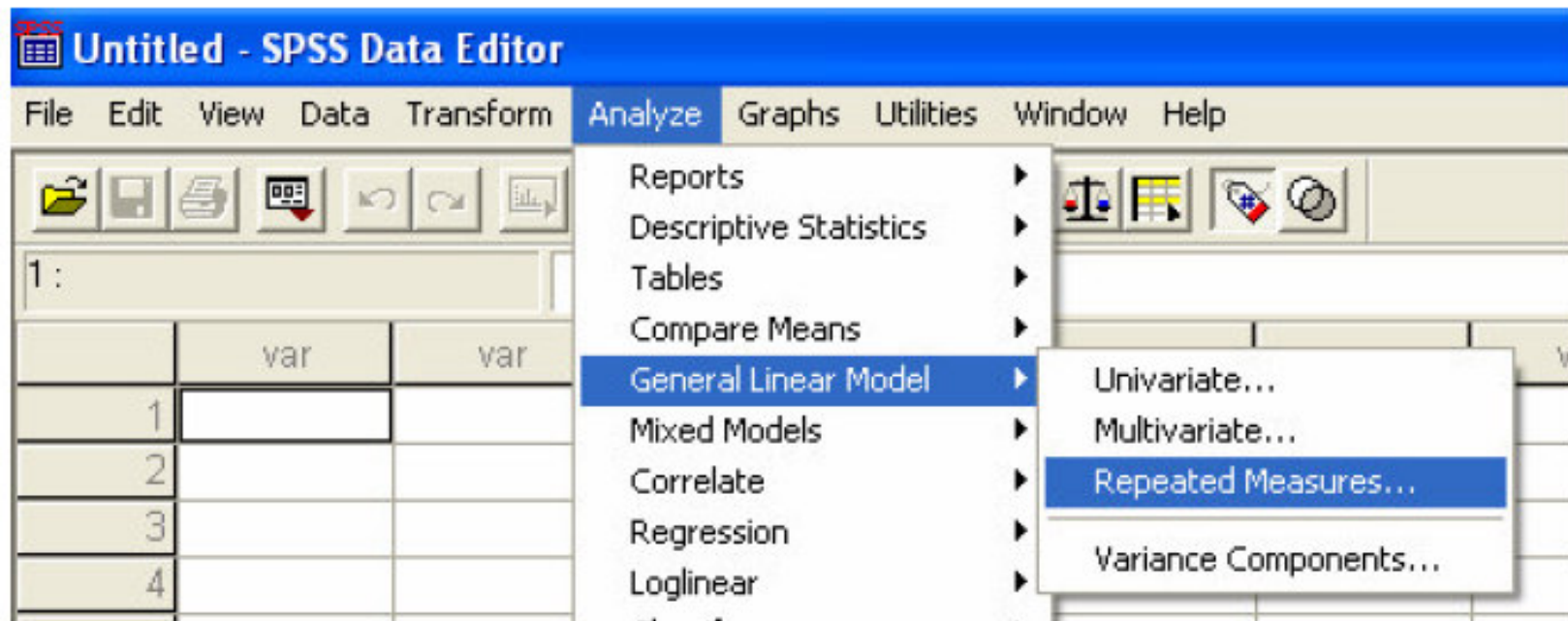
- Probability
- The percentage of times you can expect to (estimate that you will) get this large a difference by chance if the distributions are not different
- $P = .024$ means?



Probability

- Multiple tests raise the chance of Type 1 errors
- I.e., False positive
- Because they overestimate probability

Repeated measures/ SPSS





ANOVA (repeated measures)

- SPSS
- Analyze
- General Linear Model
- Repeated measures



(M)ANOVA

- H_0 : There is no difference between levels of a factor
- H_1 : There is a difference between at least one level and the others

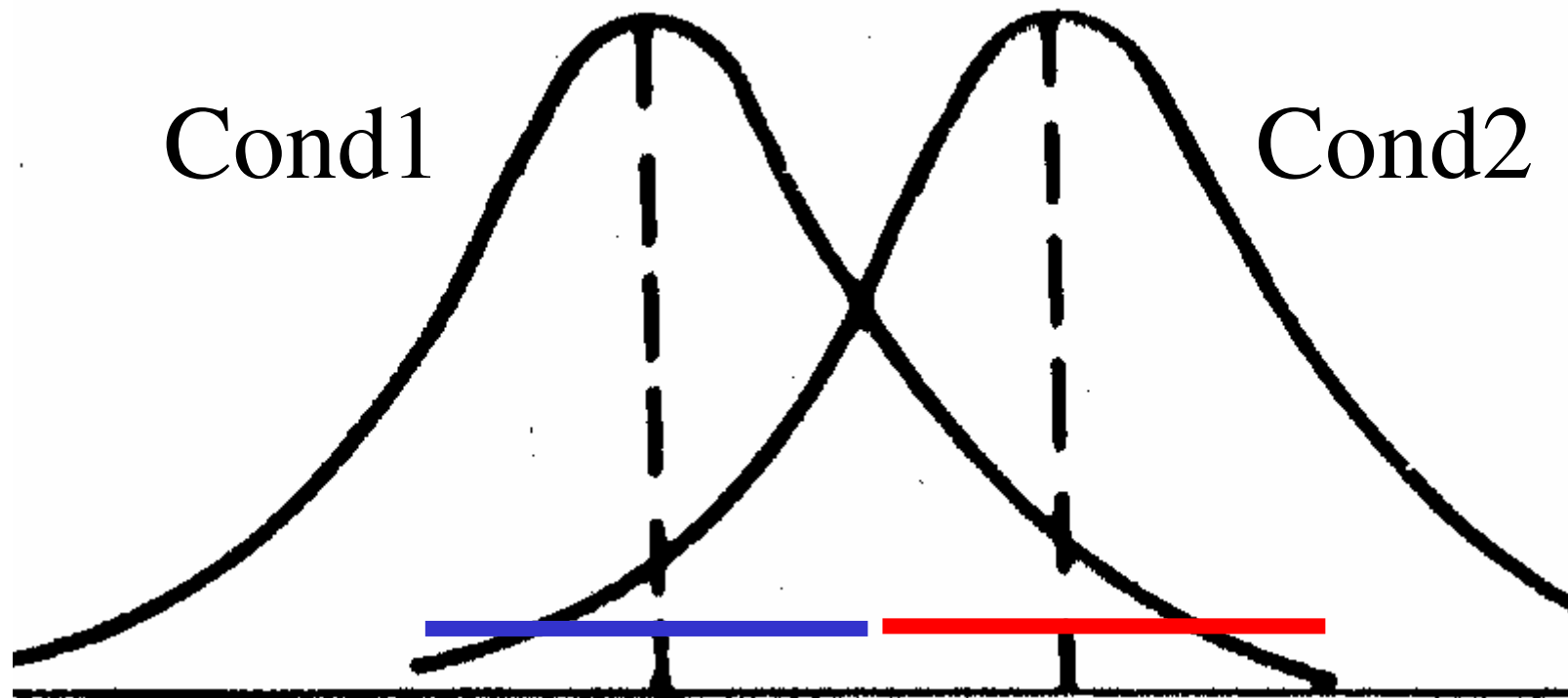


F ratio

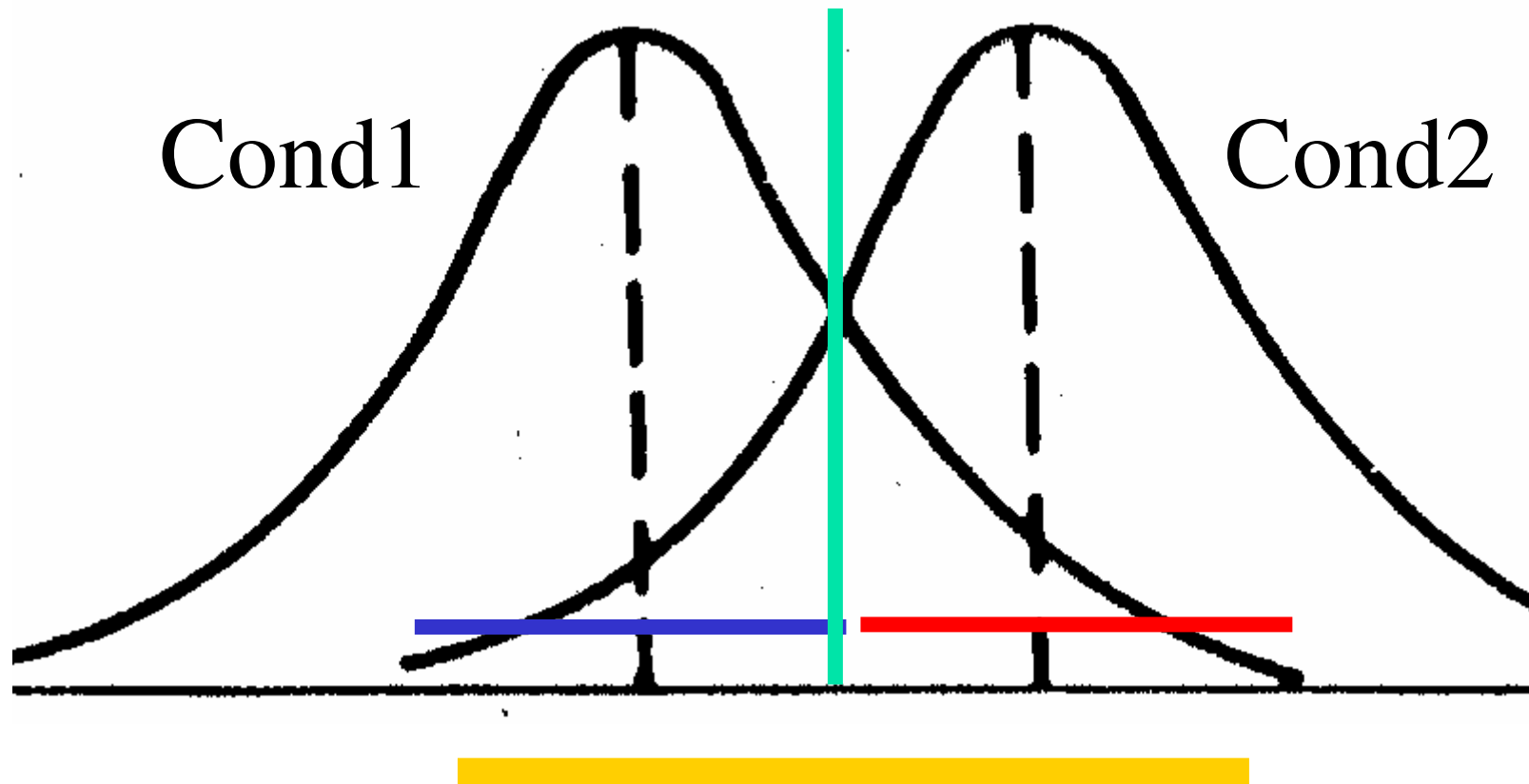
- Estimated variance given that all observations come from a single distribution
-
- Average estimated variances of each condition separately



Estimating Variance



Estimating Variance





F ratio

- Estimated variance of single distribution



- Average estimated variances of condition



F ratio

- The bigger the F-ratio



- The less likely that the conditions come from the same distribution



Experiment with three levels

Tests of Within-Subjects Effects

Measure: MEASURE_1

Source		Type III Sum of Squares	df	Mean Square	F	Sig.
context	Sphericity Assumed	2,961	2	1,480	39,786	,000
	Greenhouse-Geisser	2,961	1,834	1,615	39,786	,000
	Huynh-Feldt	2,961	1,985	1,492	39,786	,000
	Lower-bound	2,961	1,000	2,961	39,786	,000
Error(context)	Sphericity Assumed	1,712	46	,037		
	Greenhouse-Geisser	1,712	42,172	,041		
	Huynh-Feldt	1,712	45,644	,037		
	Lower-bound	1,712	23,000	,074		



Why so many tests?

- Because ANOVA and MANOVA various assumptions
 - Sphericity. For example
- And various corrections are carried out if an assumption is not valid
 - Maybe more in another presentation
 - But practically it usually does not change the significance much



Experiment with three levels

- Okay, now you know that there is an effect (at least one of the conditions is statistically different from the others)
- But that does not answer your question



Experiment with three levels

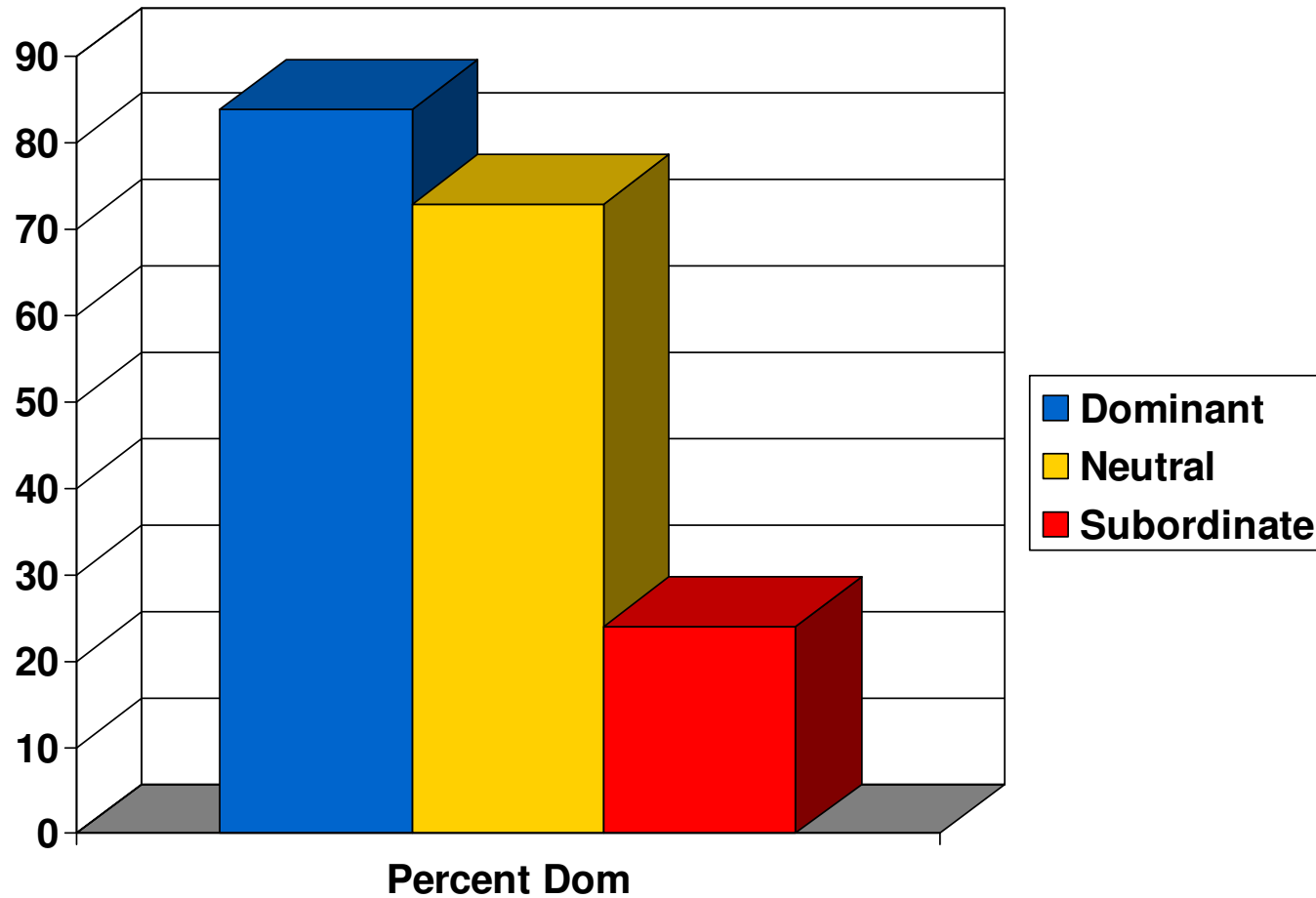
- Is there an effect of context?
- To increase completions indicating that the subordinate meaning has been selected
- To increase completions suggesting the ***dominant*** meaning has been selected?



Experiment with three levels

- The F-test shows that at least one condition is significantly different
- And you are justified in using individual *post-hoc* comparisons to test where it comes from

Percentage Dominant Response





Experiment with three levels

Paired Samples

		Paired Differences		
		Mean	Std. Deviation	Std. Error Mean
Pair 1	DOMCONT - NEUTCONT	,1149	,17421	,03556
Pair 2	SUBCONT - NEUTCONT	-,4908	,24763	,05055



Experiment with three levels

d Samples Test

Differences					
Std. Error Mean	95% Confidence Interval of the Difference		t	df	Sig. (2-tailed)
	Lower	Upper			
,03556	,0413	,1885	3,231	23	,004
,05055	-,5953	-,3862	-9,709	23	,000



MANOVA

- Like ANOVA
- in cases where more than one factor is being manipulated



Experiment with *nine* levels

- Het/de
- Akkoord / overeenkomst / melodie
- kon met weinig moeite worden_____
- kon door de politici worden_____
- kon door de pianist worden_____



Why this addition?

- To *independently* examine the effect of the context
- Really neutral, dominant supporting...?
- May steer toward one sort of completion regardless of the ambiguity



Methodological Sidestep

- How can you best judge if the completions are consistent with the dominant or subordinate meaning?



Methodological Sidestep

- Blind rating
- Non-blind overestimated the likelihood of dominant completions
- Particularly in the dominant condition



Nine Levels!

- This is the wrong way to look at the data
- Here you have two factors with three levels which combine to give you 9 conditions



Experiment with 3 x 3 design

- Ambiguity: 3 levels
 - Ambiguous
 - Dominant control
 - Subordinate Control
- Sentence context
 - Neutral
 - Dominant supporting
 - Subordinate supporting



Orthogonality

- Carry out tests that are *independent* of each other
- And thus do not lead to overestimation of probability



Orthogonality

- The answers to the following are independent, i.e. do not influence each other
- Main effect 1: $a + b = ? = c + d$
- Main effect 2: $a + c = ? = b + d$
- Interaction: $a - b = ? = c - d$



- Repeated measures
- Factor Ambiguity 3 levels add
- Factor Context 3 levels add

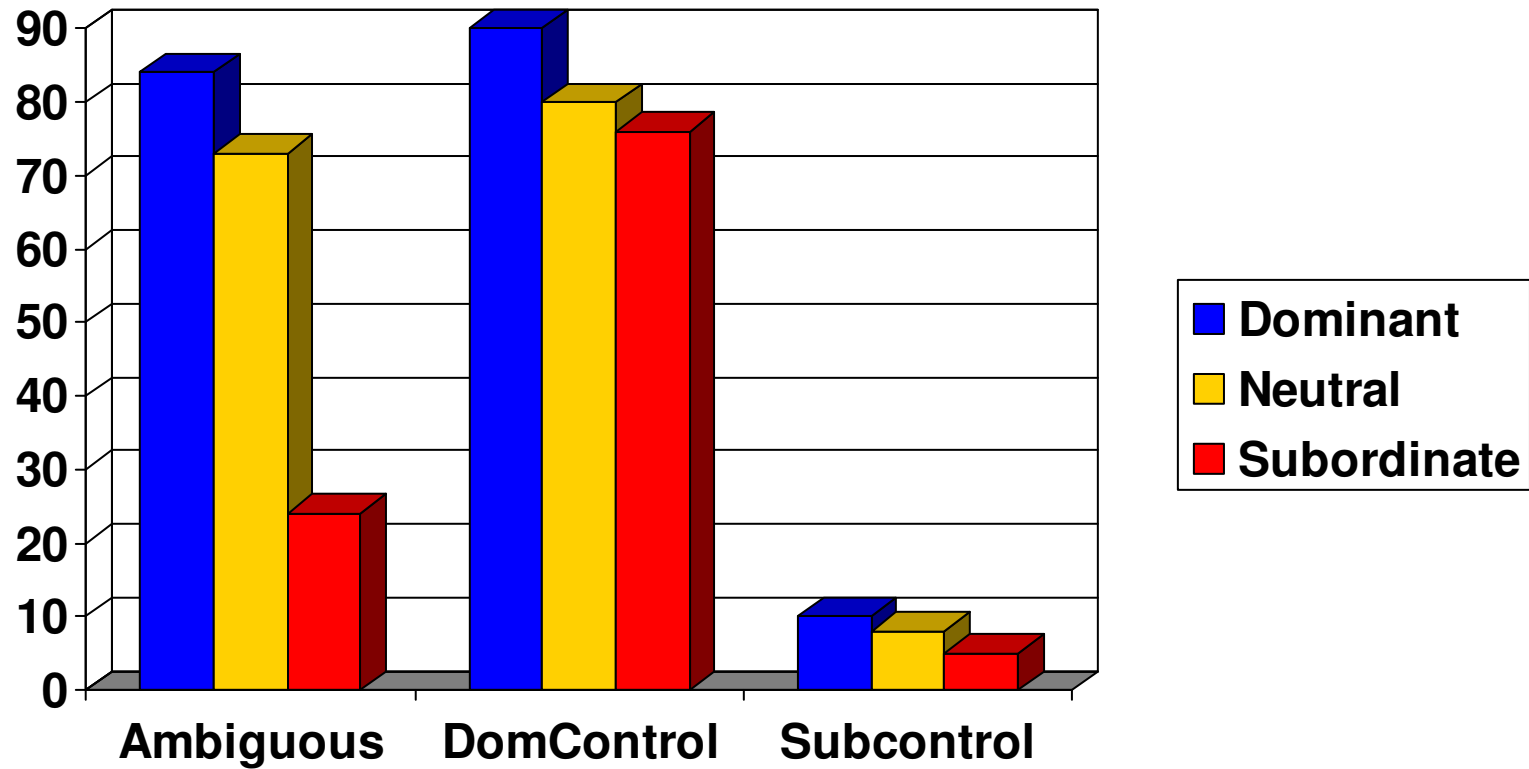
- Fill in design matrix



Matrix

- Fill in matrix with variables
 - Ambigdom (1,1)
 - Ambigneut (1,2)
 - Ambigsub (1,3)
 - Dcontdom (2,1)
 - Dcontneut (2,2)
 - Dcontsub (2,3)
 - Scontdom (3,1)
 - Scontneut (3,2)
 - Scontsub (3,3)

Percentage Dominant Response





Main Effects and Interactions

- When you have orthogonal factors you can investigate
 - main effects of each factor
 - Interactions between factors



Statistical Reasons for MANOVA

- Fragmented univariate ANOVAs lead to type 1 errors
 - seeing effects that aren't really there.
- Univariate ANOVAs throw away info - correlation among dependent variables.



Clearer Example of Interaction

- We know that both word frequency and irregularity of spelling contribute to how quickly words are recognized
- But are these effects independent of each other?
 - Repeated measures design with naming task



SPSS Output :

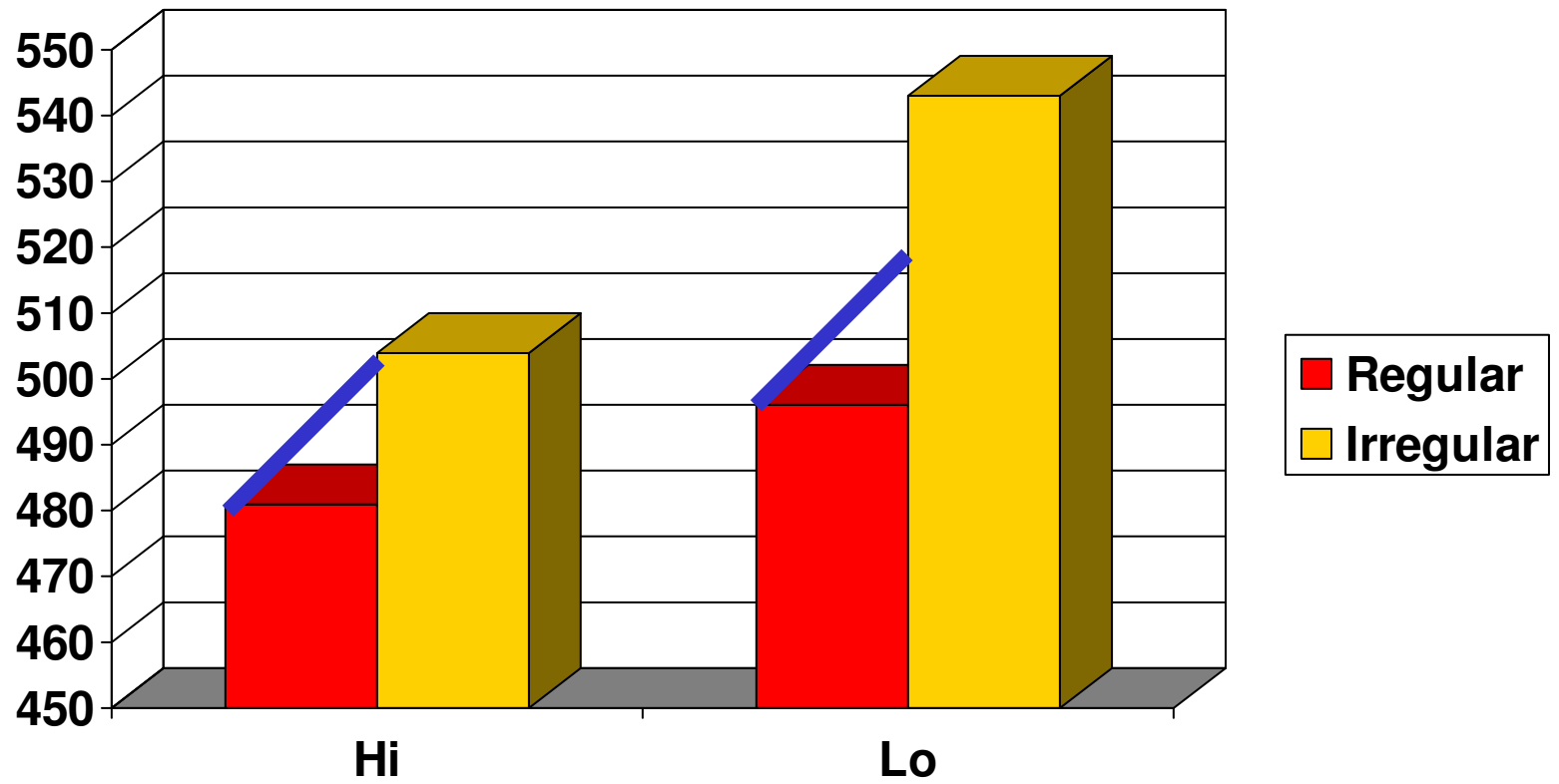
Chance to check design!

Within-Subjects Factors

Measure: MEASURE_1

reg	freq	Dependent Variable
1	1	reghi
	2	reglo
2	1	irreghi
	2	irreglo

Results





Main Effects and Interaction?

- Low frequency RTs > High Frequency?
- Irregular RTs > Regular ?
- Maybe combination is bigger than either alone?



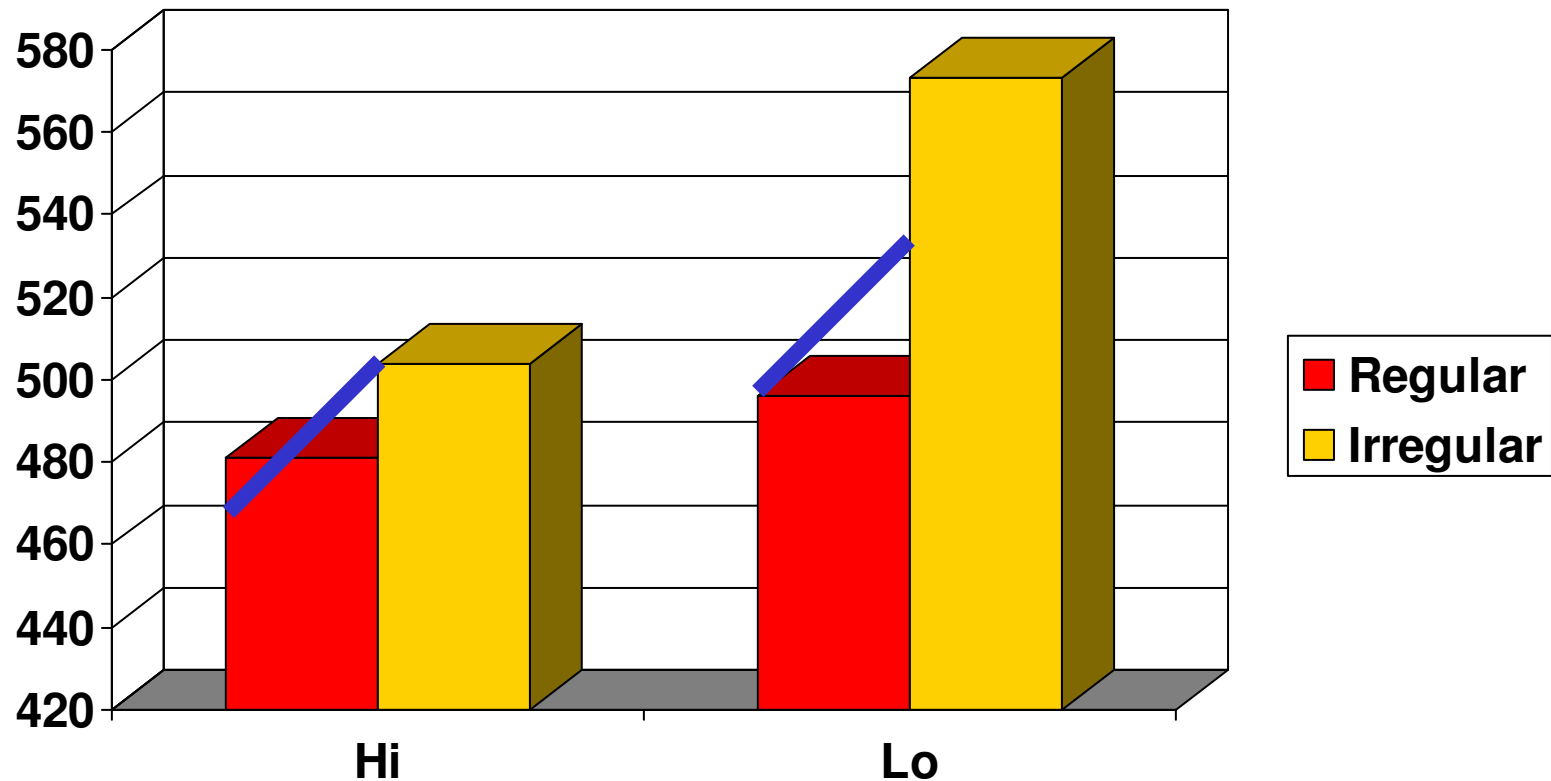
Main Effects and Interaction?

Tests of Within-Subjects Contrasts

Measure: MEASURE_1

Source	reg	freq	Type III Sum of Squares	df	Mean Square	F	Sig.
reg	Linear		19321,000	1	19321,000	34,966	,000
Error(reg)	Linear		8288,500	15	552,567		
freq		Linear	11881,000	1	11881,000	14,079	,002
Error(freq)		Linear	12658,500	15	843,900		
reg * freq	Linear	Linear	2475,063	1	2475,063	2,329	,148
Error(reg*freq)	Linear	Linear	15940,438	15	1062,696		

Results: More like real results





Main Effects and Interaction?

Tests of Within-Subjects Contrasts

Measure: MEASURE_1

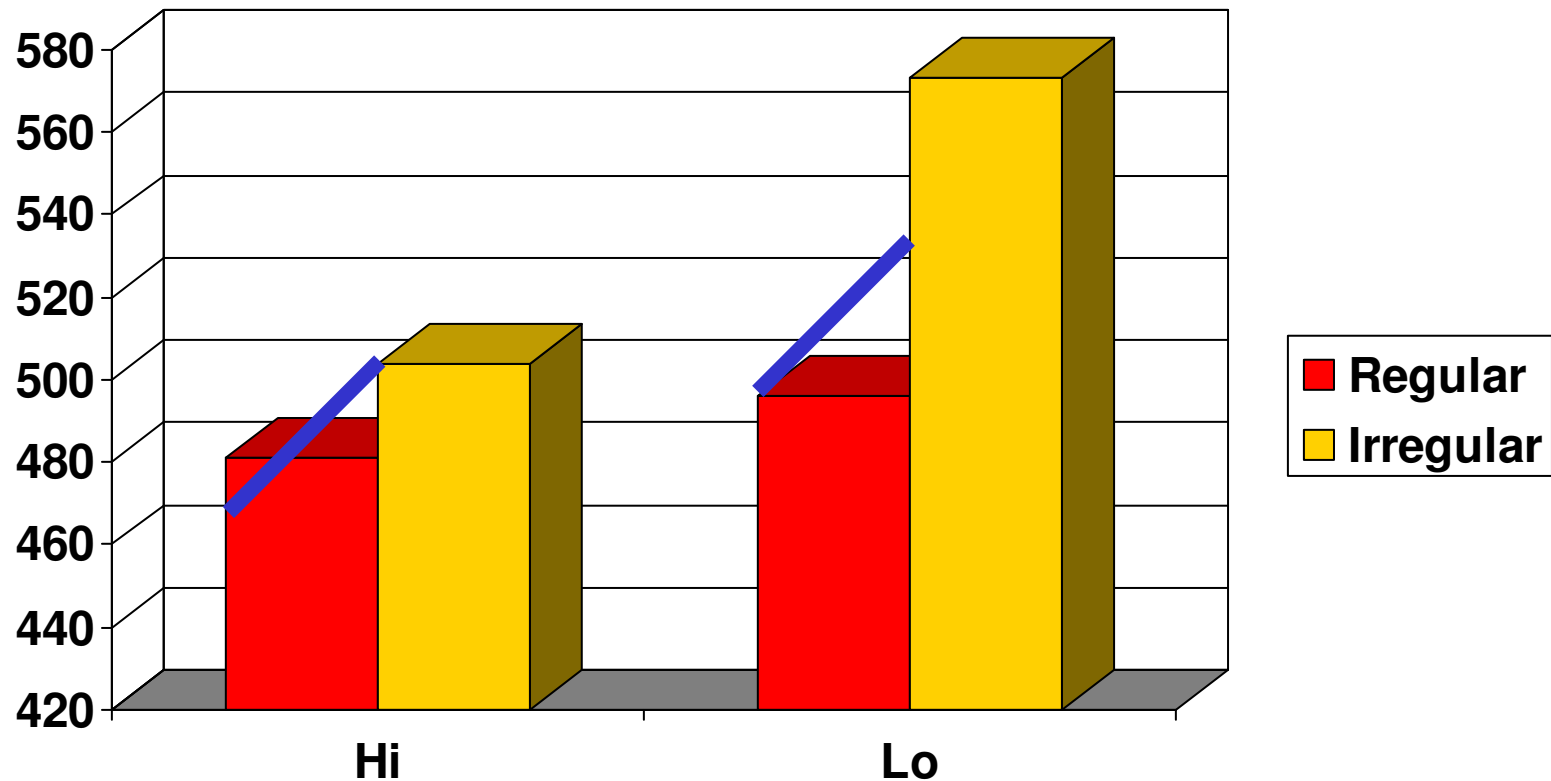
Source	reg	freq	Type III Sum of Squares	df	Mean Square	F	Sig.
reg	Linear		39601,000	1	39601,000	63,463	,000
Error(reg)	Linear		9360,000	15	624,000		
freq		Linear	28561,000	1	28561,000	31,178	,000
Error(freq)		Linear	13741,000	15	916,067		
reg * freq	Linear	Linear	12045,063	1	12045,063	10,825	,005
Error(reg*freq)	Linear	Linear	16690.938	15	1112.729		



What are main effects and interactions?

- The difference between the differences
- Main effect 1: $a + b = ? = c + d$
- Main effect 2: $a + c = ? = b + d$
- Interaction: $a - b = ? = c - d$

Results: More like real results





What is an interaction?

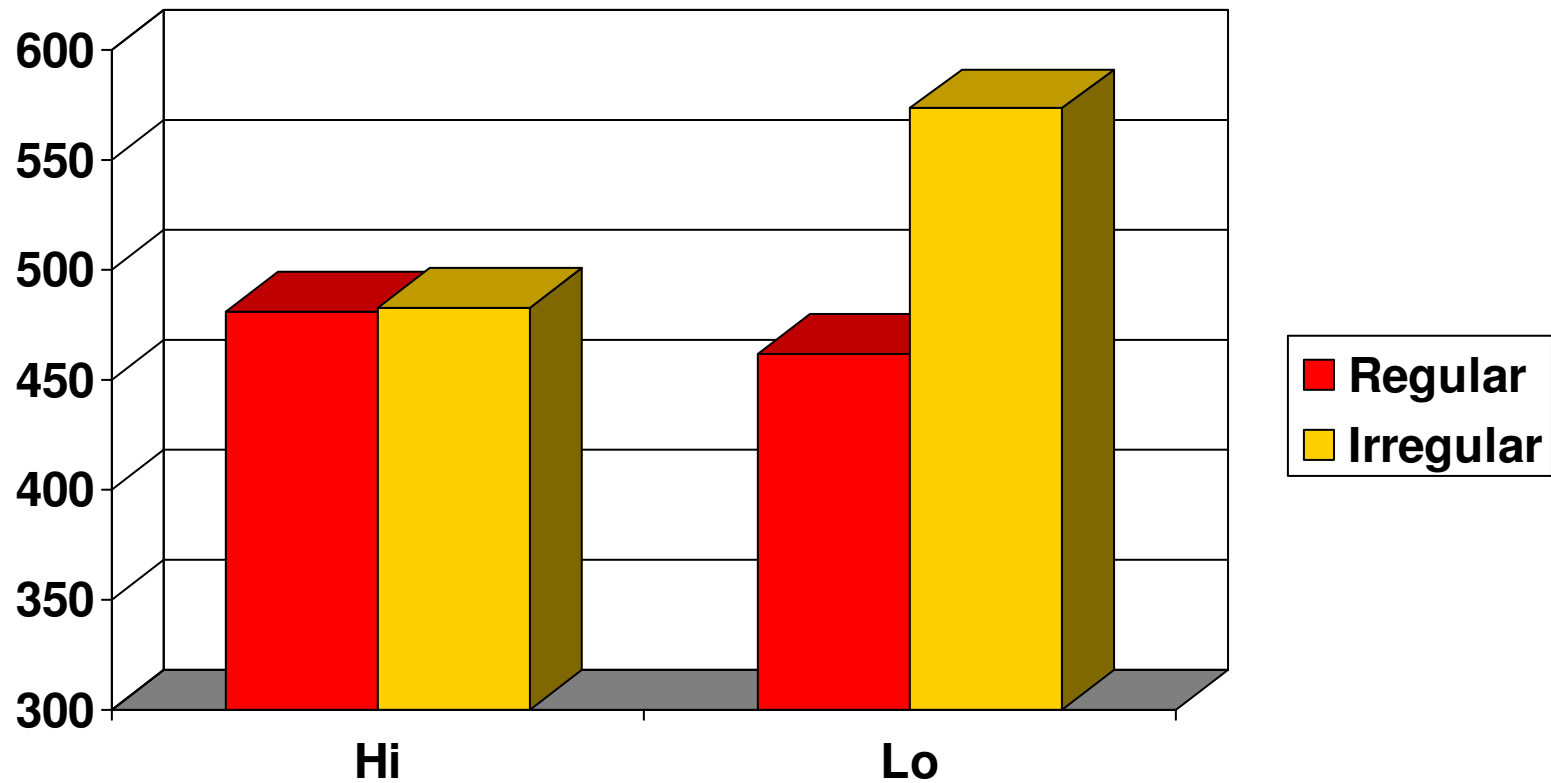
- The difference between the differences
- Main effect 1: $(a + b) - (c + d) = ? = 0$
- Main effect 2: $(a + c) - (b + d) = ? = 0$
- Interaction: $(a - b) - (c - d) = ? = 0$



Main Effects and Interaction?

- If there is an interaction between regularity and frequency
- What can we conclude about the effects of regularity and frequency?
 - Can't be sure that they are not due to the interaction

Results: More like real results





Main Effects and Interaction?

- How can we best interpret the interaction between regularity and frequency and the main effects
- Post-hoc analyses



Interaction/main effect posthocs

Paired Samples Test

		Paired Differences			
		Mean	Std. Deviation	Std. Error Mean	95% C Interv Diff
Pair 1	reghi - reglo	-14,81250	9,33251	2,33013	-19,78545
Pair 2	reghi - irreghi	-22,31250	27,66639	6,91060	-37,05488



Interaction/main effect posthocs

Paired Samples Test

Differences			t	df	Sig. (2-tailed)
Mean	95% Confidence Interval of the Difference				
	Lower	Upper			
2,33313	-19,78545	-9,83955	-6,349	15	,000
5,91660	-37,05488	-7,57012	-8,226	15	,006



Interaction/main effect posthocs

- Frequency and regularity both have effects (< posthocs)
- But the combination of the two leads to greater difficulty than just the sum of the two effects (< existence of interaction)



Assumptions of MANOVA

- Independence of observations (as in univariate ANOVA)
- Multivariate normality - all dependent variables and linear combinations of them are distributed normally
- Equality of covariance matrices (cf homogeneity of variance in univariate)



Assumptions of MANOVA

- Second and third assumptions are more stringent than corresponding univariate assumptions in univariate ANOVA.