

Linear Discriminant Analysis



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RUG

Goals of this presentation

- Insight in Discriminant analysis
 - When to use it
 - How to use it
- Critical review of a dialectological method
 - Be careful with native raters!



Route map

- Swiss Standard German long <ä>
 - [ɛ:]~[e:] variation
- Methodology
 - Corpus
 - On line experiment: Level of Swiss accent
 - Categorical analysis
 - Acoustical
- Statistics: Discriminant Analysis
- Results



Standard German <ä>

- Träne ‘Tear’
- Räd-chen ‘wheel.Dim’
- Bäder ‘bath.Plur’
- fähr-t ‘drive.3Sg’



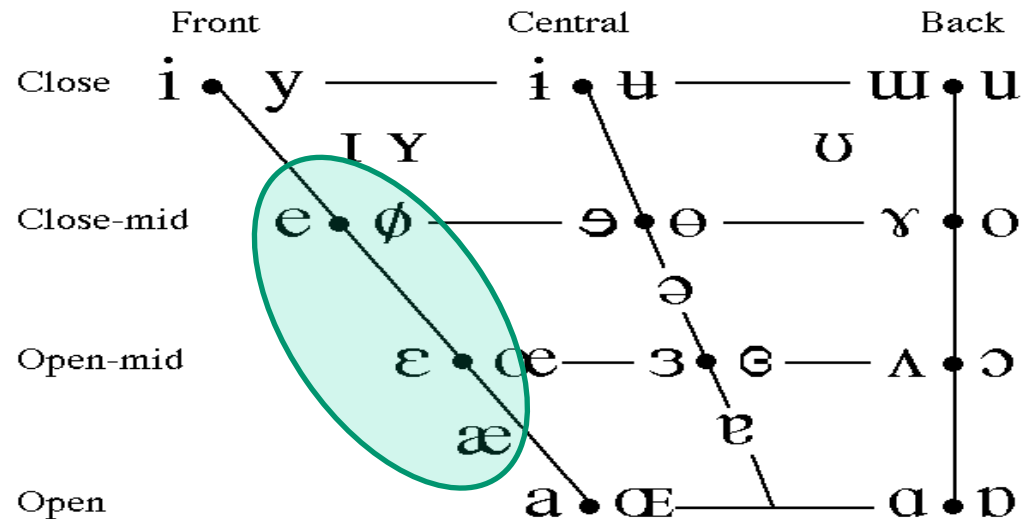
[ε:]~[e:] Variation

- Träne tr[e:]ne~tr[ε:]ne
- Räd-chen r[e:]dchen~ r[ε:]dchen
- Bäder b[e:]der~ b[ε:]der
- fähr-t f[e:]rt~ f[ε:]rt



[ɛ:]~[e:] Variation

- The [ɛ:]~[e:] variation is gradient
any realization between [ɛ:]~[e:] is possible



Where symbols appear in pairs, the one to the right represents a rounded vowel.



Swiss Standard German (SSG)

- Swiss Standard German (SSG) differs from Standard German as spoken in Germany (NSG)
 - E.g. in NSG <ä> is more likely to be pronounced as [e:]

- Neutralization with <e>

» Beeren b[e:]ren ‘berry.Plur’

» Bären b[e:]ren ‘bear.Plur’

– SSG ‘Schriftsprache’

- Close connection orthography and pronunciation

» Beeren b[e:]ren ‘berry.Plur’

» Bären b[ɛ:]ren ‘bear.Plur’



Swiss Standard German (SSG)

- Change?
 - Younger speakers tend to a more NSG pronunciation
 - Older speakers tend to a more SSG pronunciation
 - Ongoing change (Hove 2002)



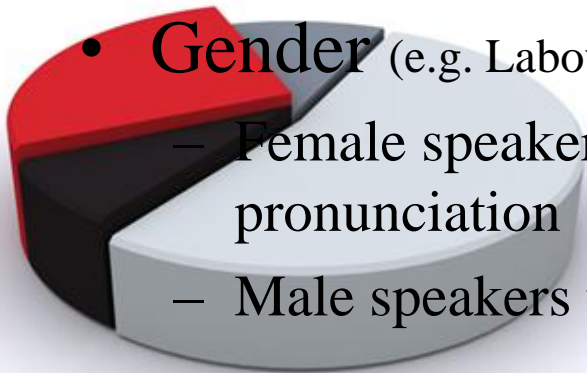
Research Question (1)

- Which factors play a role in the realization of <ä> in Swiss Standard German?



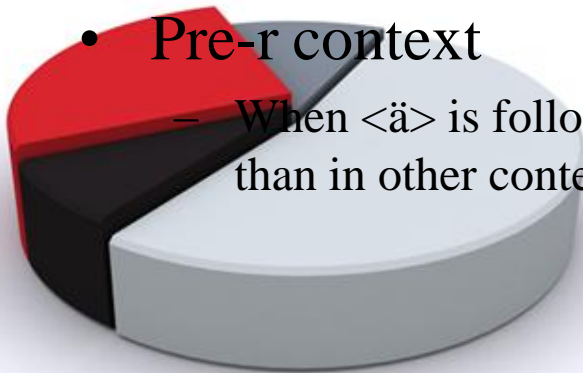
Hypotheses

- **Swiss accent**
 - The more Swiss accent a speaker has, the lower (i.e. [ɛ:] -like) the realization of <ä>
- **Age** (e.g. Labov 2001)
 - Younger speakers tend to a higher (i.e. [e:] -like) pronunciation
 - Older speakers tend to a lower (i.e. [ɛ:] -like) pronunciation
- **Gender** (e.g. Labov 2001)
 - Female speakers tend to a higher (i.e. [e:] -like) pronunciation
 - Male speakers tend to a lower (i.e. [ɛ:] -like) pronunciation



Hypotheses

- Umlaut
 - <ä> that is the result of umlaut of <a> has a lower (i.e. [ɛ:]-like) realization
- Frequency (Bybee 1999 et seq., Phillips 2006)
 - Words that are highly frequent are likely to be pronounced with a lower (i.e. [ɛ:]-like) pronunciation
 - Words that are lowly frequent are likely to be pronounced with a higher (i.e. [e:]-like) pronunciation
- Pre-r context
 - When <ä> is followed by a rhotic, pronunciation is lower (i.e. [ɛ:]-like), than in other contexts (Hall 1990)



Methodology

- Recordings of ‘native speakers’
- Categorical rating by two linguistically trained ‘native speakers’
- Logistic regression test on the factors
- *Common method, but reliable?*



Psycholinguistics:
Listeners reconstruct
what they think they
hear.....

Research Question (2)

- Do raters rely on just acoustic features?
= are raters objective and unbiased?



Methodology

- Raters' judgements compared with the acoustical measurements
 - Are the [e:] and [ɛ:] ratings clear-cut categories?



Level of SSG accent

- Corpus data
 - Institut für deutsche Sprache Mannheim
(Brinckmann et al. 2008)
 - 40 speakers
 - Average 15 <ä> per speaker
 - 22 males 18 females
 - 7 locations



Level of SSG accent

- Online elicitation of the level of Swiss accent of all speakers in the corpus
 - 40 respondents: 20 German 20 Swiss
 - Estimation of the SSG accent on a four-point scale
 - <http://wievielstandardspracheinderschweizb.yolasite.com/>



Raters judgements

- Two raters
 - Both female
 - 24 and 27 years old
 - Linguistically trained
 - Judged long <ä> to be pronounced as either [e:] or [ɛ:]

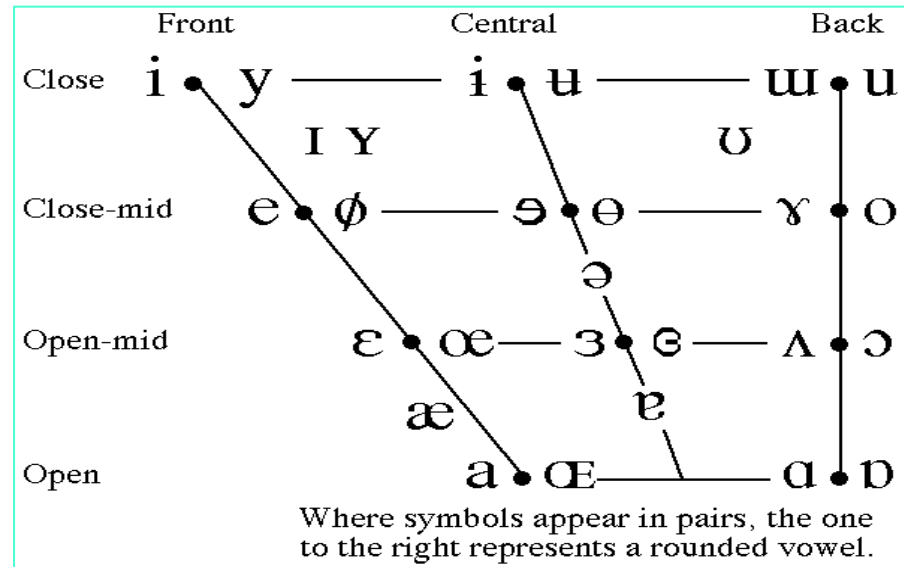


Acoustical analysis

- First formant F1 and second formant F2 were measured in Praat (Weenink & Boersma 2010)



F1



F2

Linear Discriminant Analysis

- Analyses whether the value of the dependent variable can be predicted on the basis of the independent variable
- Parametric test
- Dependent variable is nominal
- Independent variable is rational



Linear Discriminant Analysis

- Aims:
 - Investigate the differences between groups
 - Predicting the category to which a value belongs
 - To determine the best way to distinguish between groups
 - Classify cases into groups



Data

Item	Rater RB	Rater MS	F1	F2
3412	E	E	4.79	11.84
3413	E	E	4.76	11.82
3414	E	E	4.70	11.74
3415	E	E	4.31	12.56
3416	e	e	5.12	11.66
3417	E	E	4.62	13.12
3418	E	E	4.85	12.12
3419	e	E	3.72	12.35
3420	E	E	4.97	12.29
3421	E	E	4.55	11.32
3422	E	E	5.49	11.63
3423	E	E	4.73	11.82
3424	E	E	4.13	12.74
3412	E	E	4.79	11.84

LDA rater 1

Call: lda(RealRB ~ F1 + F2, data = CH)

Prior probabilities of groups:

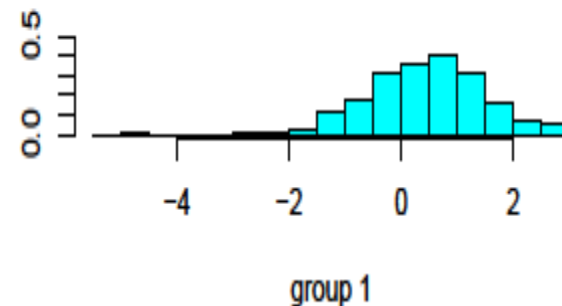
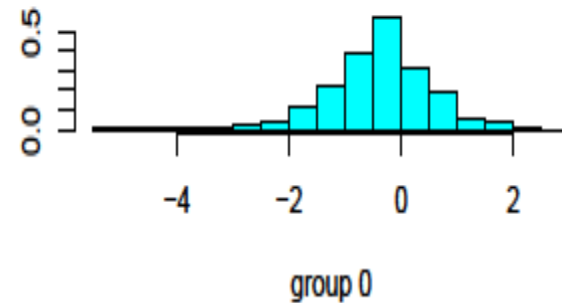
0	1
0.685567	0.314433

Group means:

	F1	F2
E	5.23	12.55
e	4.73	13.11

Coefficients of linear discriminants:

LD1
F1 -0.82
F2 0.77



LDA rater 2

Call: lda(RealMS ~ F1 + F2, data = CH)

Prior probabilities of groups:

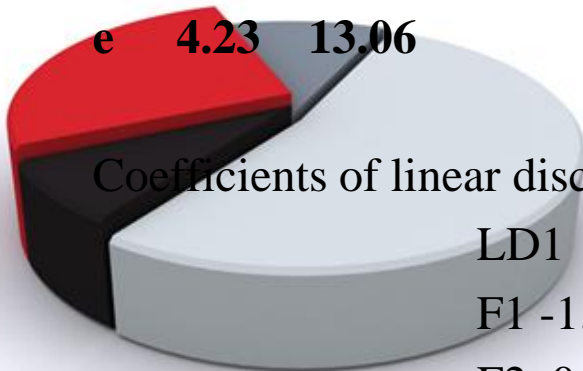
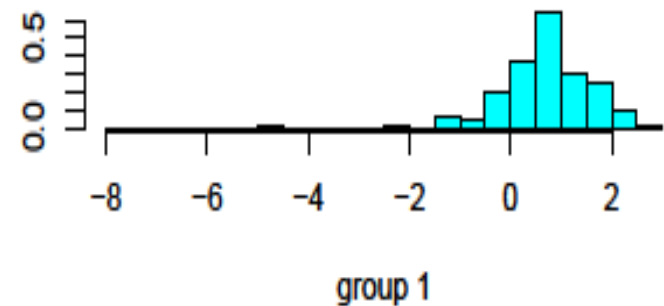
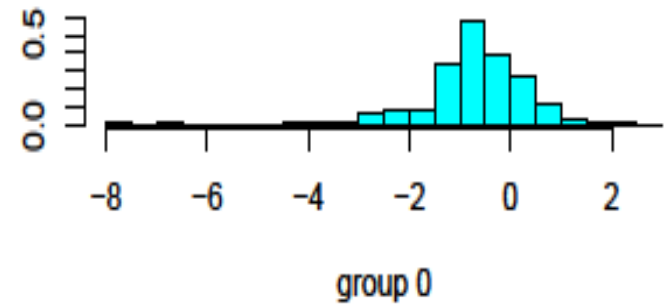
0	1
0.806563	0.193437

Group means:

	F1	F2
E	5.28	12.65
e	4.23	13.06

Coefficients of linear discriminants:

LD1	
F1	-1.0583420
F2	0.5133036



LDA pairs of ratings

ee

F1

F2

N 5.24

12.66

Y 4.17

13.09

EE

F1

F2

N 4.70

13.07

Y 5.28

12.53

eE

F1

F2

N 5.03

12.65

Y 5.28

13.11

Ee

F1

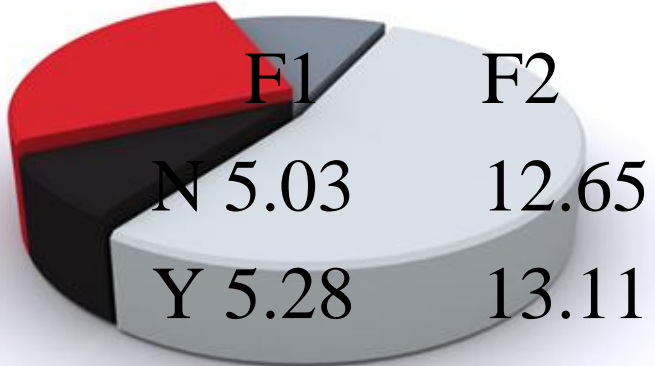
F2

N 5.10

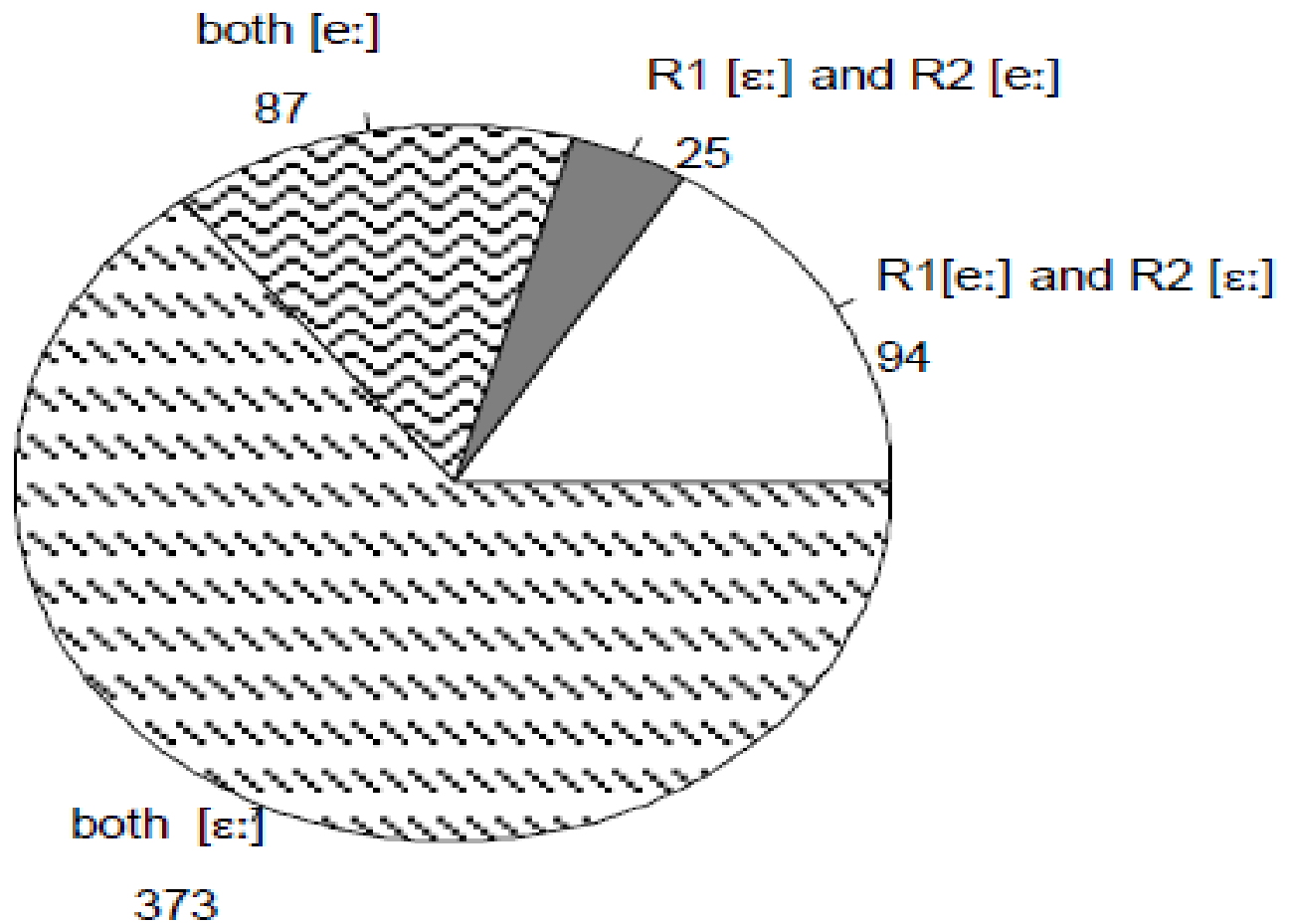
12.72

Y 4.50

12.85



LDA pairs of ratings



Further....

- Comparison
 - Logistic regression on the raters data
 - Linear regression on the acoustic measurements
- Totally different analysis!



Further....

- Raters' judgements are predictable by SSG accent level and pre-r context
- Acoustic measurements are predictable by other factors.....



Further....

	Estimate	Std. Error	t value	p-value
(Intercept)	64.51	3.588	17.98	< .001*
Age young	-7.63	1.342	-5.69	< .001*
Gender male	5.70	1.247	4.57	< .001*
LogLemmaFrequency	0.03	1.382	0.03	0.978
Pre-r context	5.03	5.497	0.92	0.361
LogLemmaFrequency : Pre-r context	-5.78	2.080	-2.78	0.006*

Residual standard error: 14.55 on 568 degrees of freedom

(2 observations deleted due to missingness)

Multiple R-squared: 0.2686, Adjusted R-squared: 0.2544

F-statistic: 18.96 on 11 and 568 DF, p-value: < 0.001

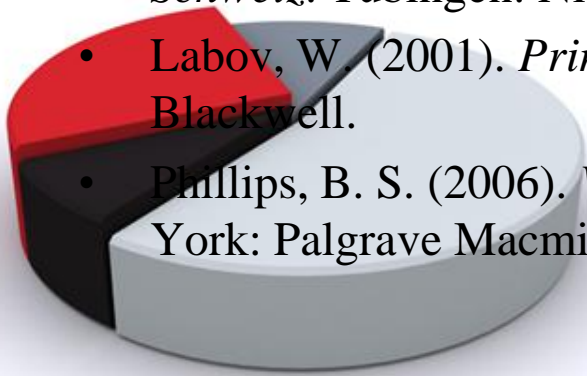
Take home message

- Don't trust the native speaker!
- Don't rely only on LDA!



References

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Discussion?

Thank you!



Acoustical analysis

- Vowels are normalized

- [i] = 100

- [a] = 0

- Euclidean distance

$$\text{Interpol} = \frac{\delta(\langle \ddot{a} \rangle - a)}{\delta(i-a)} * 100$$



prototypical [ɛ] = 56

prototypical [e] = 72