

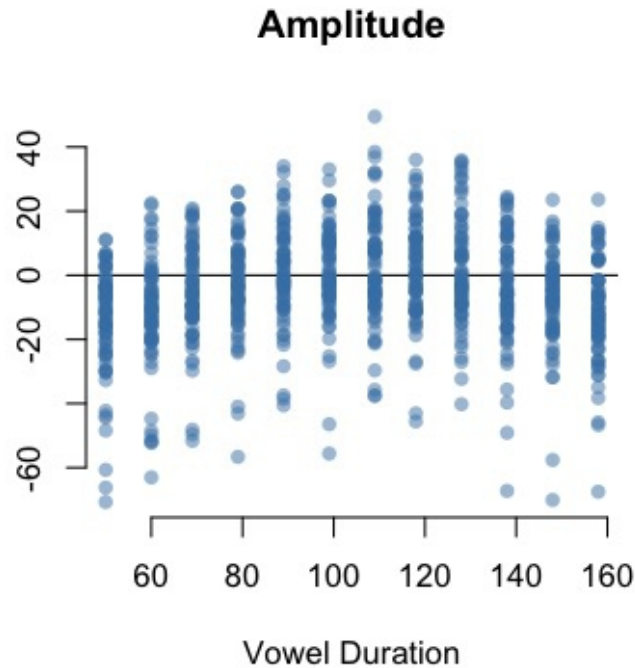


1. Linear regression



Example data

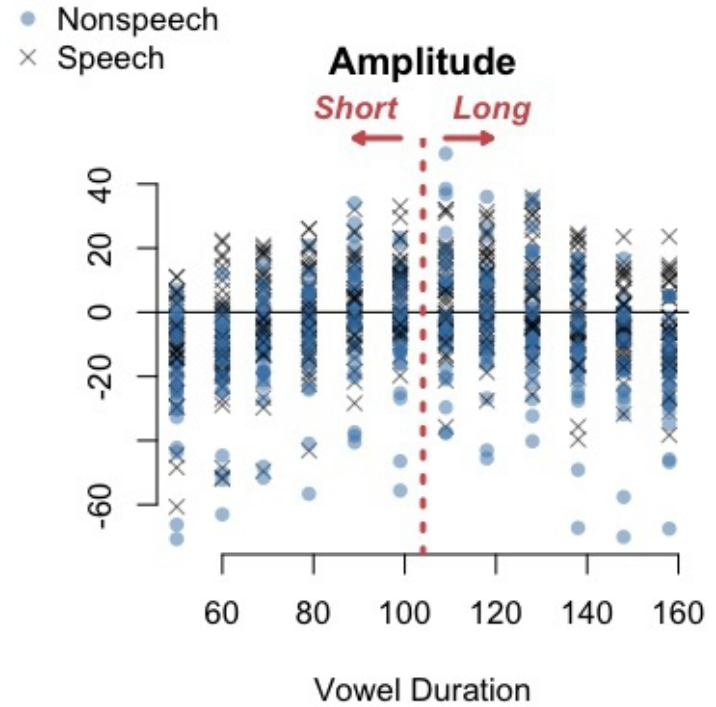
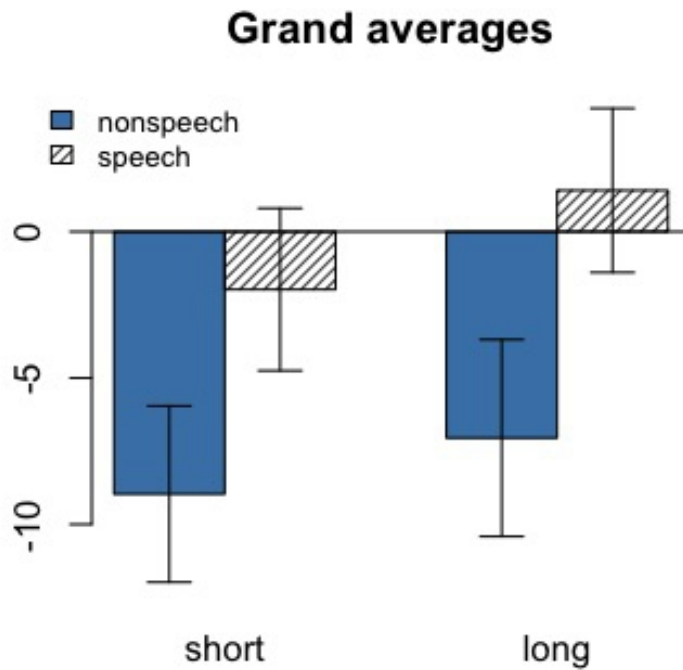
- MEG data of Tomaschek et al. (2013)
 - *Vowel duration and mode*





ANOVA

- Categorical data





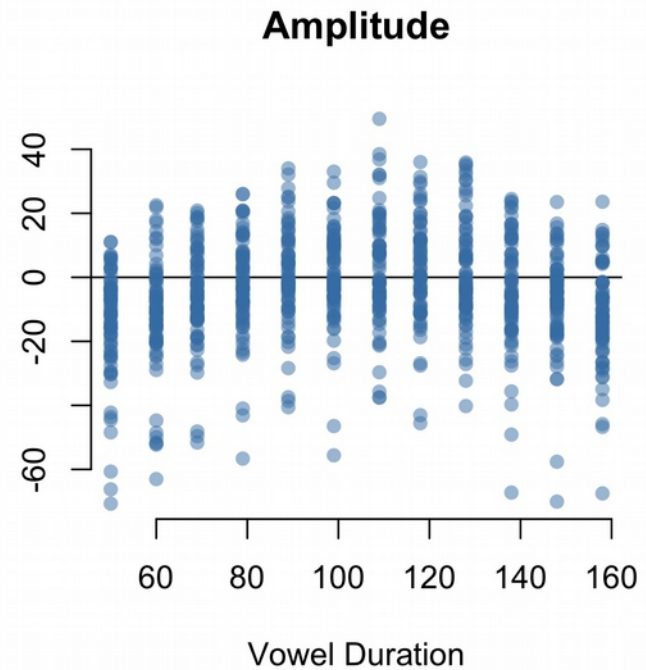
Linear regression

- Continuous and categorical predictors

- Example 1:

Could the value of *Vowel Duration* explain the measured *Amplitude*?

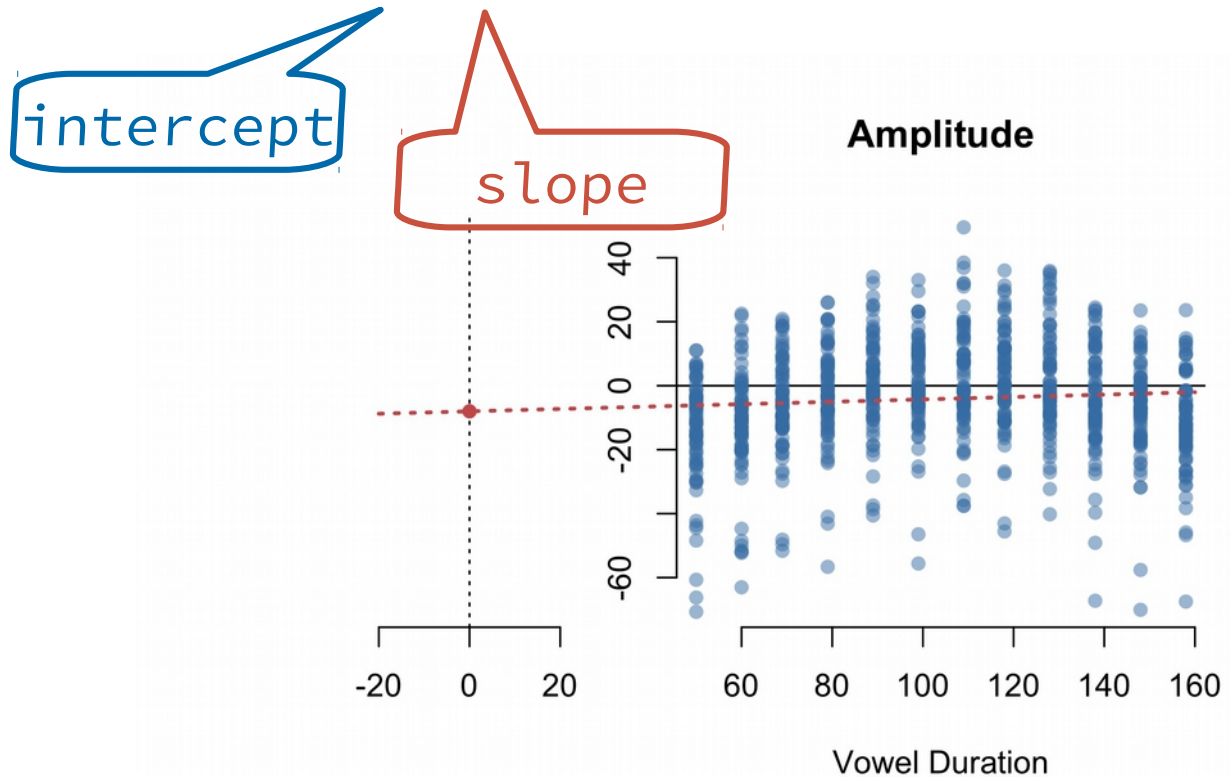
- Vowel duration = numeric





Continuous predictors

- Regression formula: $y = \beta_0 + \beta_{VD} * x + \epsilon$





Continuous predictors

- Regression formula: $y = \beta_0 + \beta_{VD} * x + \epsilon$

```
lm1 <- lm(Amp ~ VD, data=dat)
summary(lm1)
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-8.01569	1.78739	-4.485	8.24e-06
VD	0.03730	0.01638	2.277	0.023



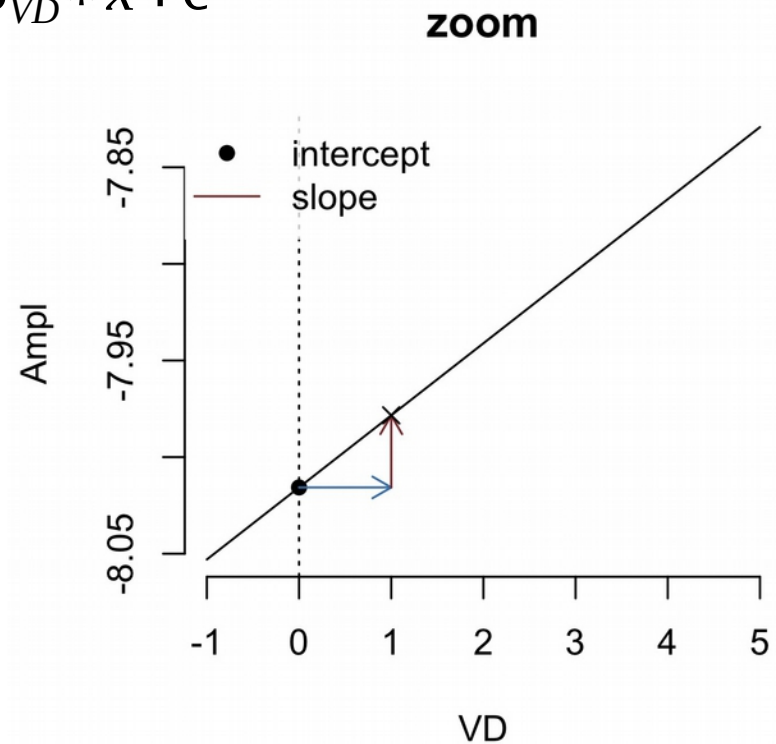
Intercept and slope

■ Regression formula: $y = \beta_0 + \beta_{VD} * x + \epsilon$

■ β_0 = Intercept: value of y when $x=0$ (crossing with y -axis)

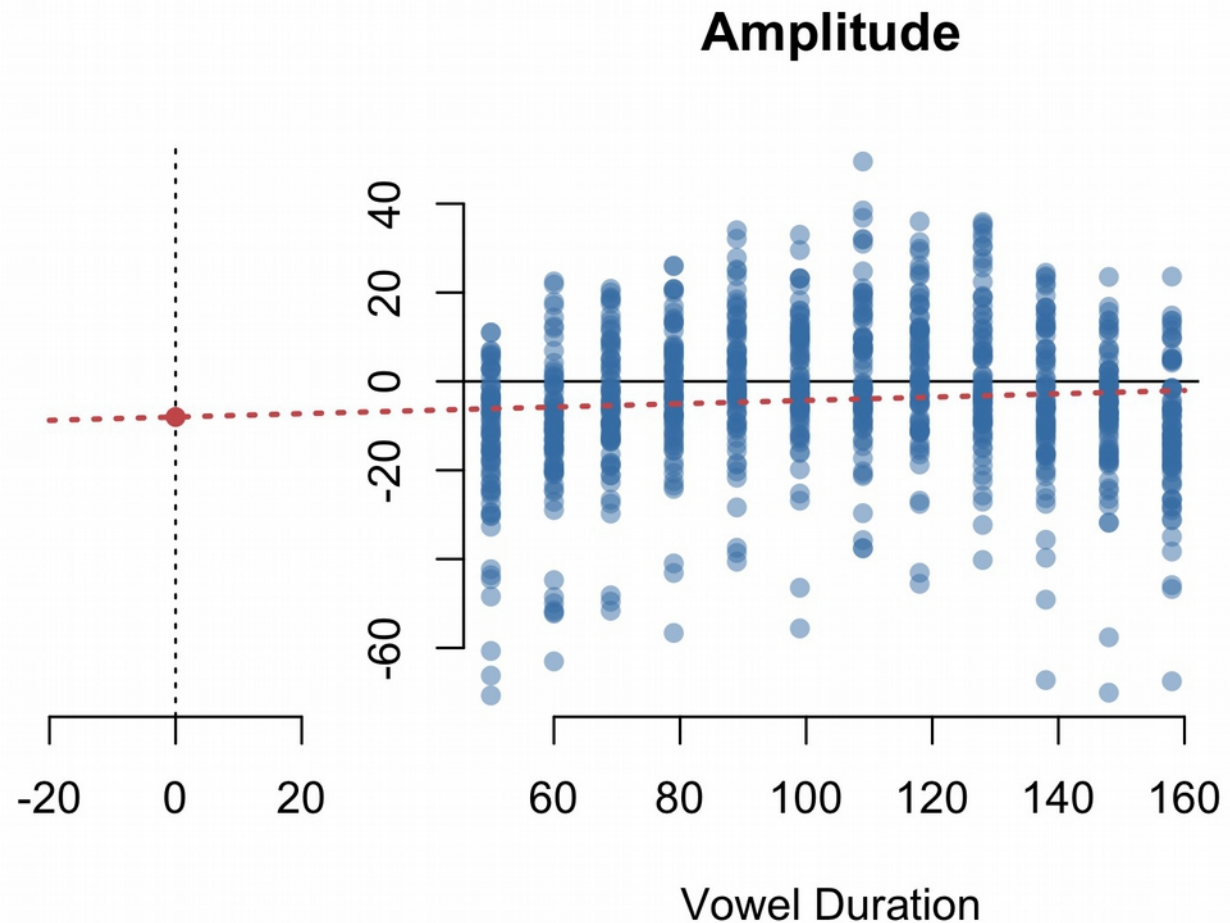
■ β_1 = Slope: change in y -value with increasing 1 unit on x -axis

■ $Y = -8.02 + 0.03730 * VD$





Intercept and slope





Categorical predictors

- *Mode*: “speech”, “nonspeech”
- Regression formula: $y = \beta_0 + \beta_{VD} * x_{VD} + \beta_{Mode} * x_{Mode} + \epsilon$

- Contrast coding

```
contrasts(dat$Mode)
```

```
sp
```

```
ns 0
```

```
sp 1
```



Categorical predictors

- Regression formula: $y = \beta_0 + \beta_{VD} * x_{VD} + \beta_{Mode} * x_{Mode} + \epsilon$

```
lm2 <- lm(Amp ~ VD+Mode, data=dat)
summary(lm2)
```

Coefficients:

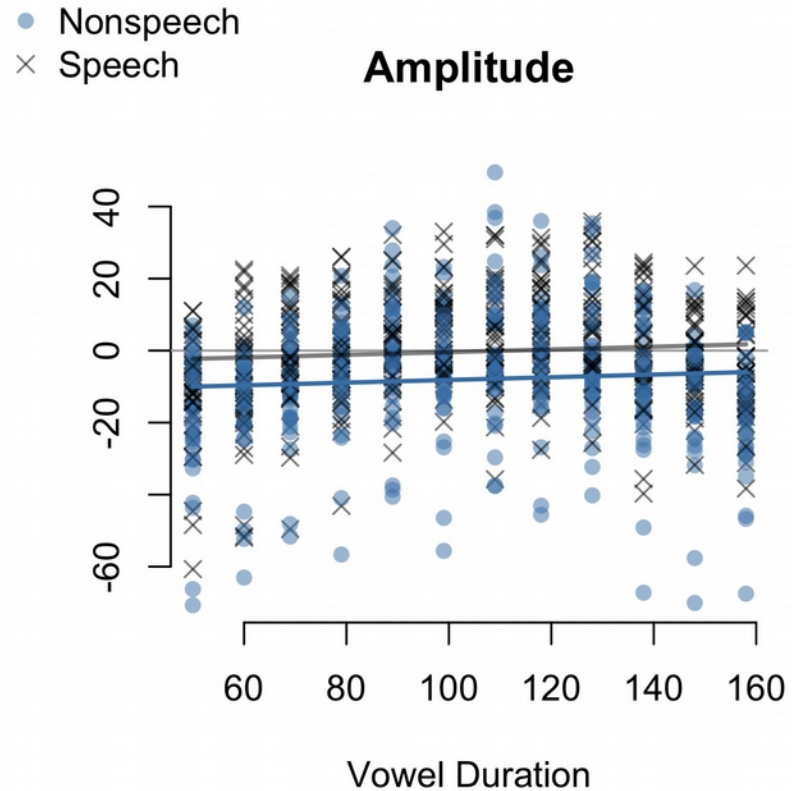
	Estimate	Std. Error	t
(Intercept)	-11.87865	1.82184	
VD	0.03730	0.01594	
Modesp	7.72592	1.07965	

```
if Mode == "ns":
    x_Mode = 0
    + 0
if Mode s=="sp":
    x_Mode = 1
    + 7.72
```



Categorical predictor

- Two regression lines:
 - Same effect of duration,
 - but difference in average amplitude between the two conditions:





Interaction

```
lm3 <- lm(Ampl ~ VD*Mode, data=dat)
#      == lm(Ampl ~ VD + Mode + VD:Mode, dat)
```

```
summary(lm3)
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-9.87585	2.46014	-4.014	6.45e-05
VD	0.01799	0.02254	0.798	0.425
Modesp	3.72032	3.47916	1.069	0.285
VD:Modesp	0.03861	0.03188	1.211	0.226



Interaction

- Testing for significance:

anova(lm2, lm3)

Analysis of Variance Table

Model 1: `Ampl ~ VD + Mode`

Model 2: `Ampl ~ VD * Mode`

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	909	241581				
2	908	241192	1	389.6	1.4667	0.2262



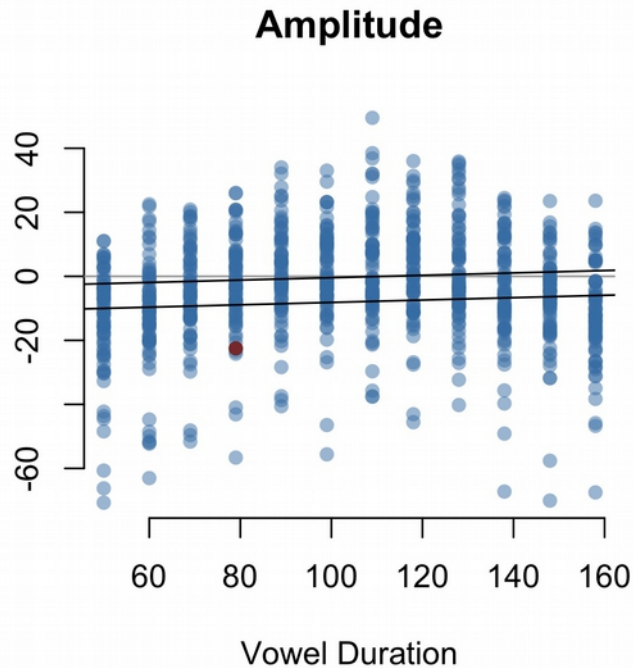
Fitted values and residuals

- Regression formula: $y = \beta_0 + \beta_{VD} * x_{VD} + \beta_{Mode} * x_{Mode} + \epsilon$
- Regression model tries to predict how the predictors influence the values of response variable
 - Fitted values: explained part of data
 - Residuals: unexplained part of data
 - ▶ Should be gaussian distributed $\epsilon \sim N(0, \sigma)$
 - ▶ No structure in residuals



Model criticism

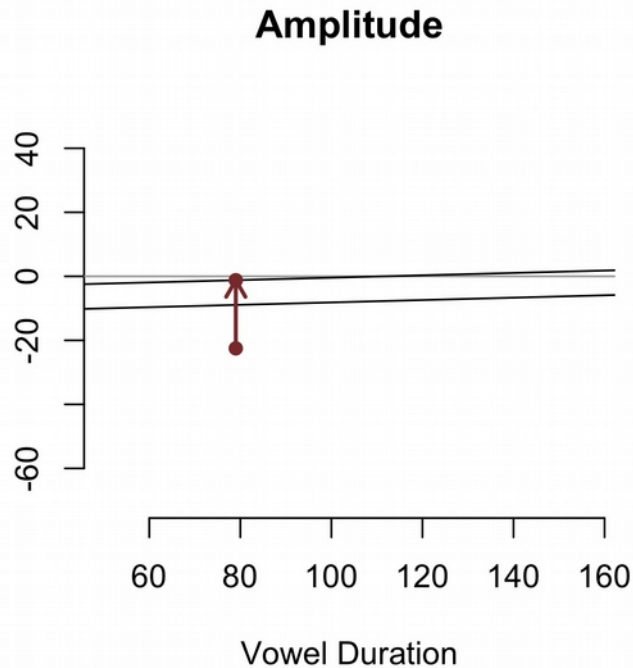
- Inspection of residuals: Comparing the fitted values with the actual data





Model criticism

- Inspection of residuals: Comparing the fitted values with the actual data

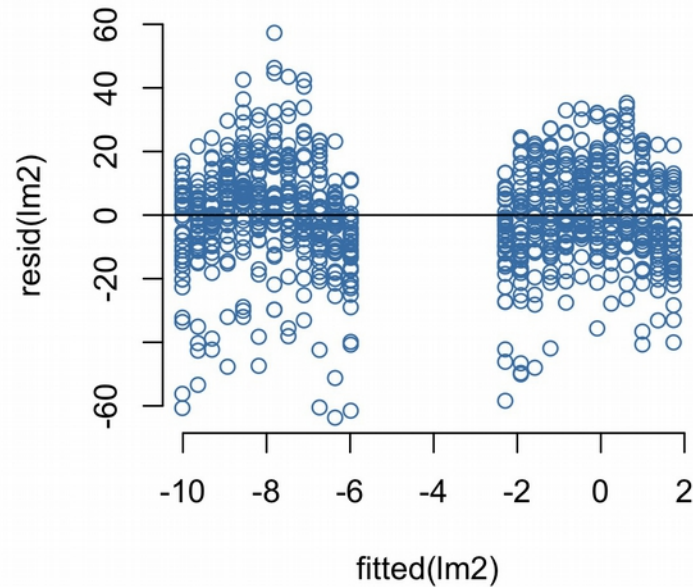
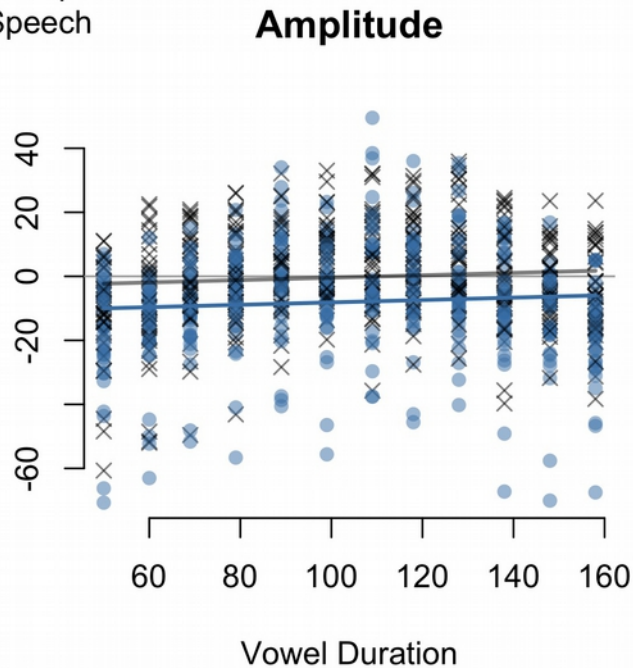




Model criticism

- Inspection of residuals: Comparing the fitted values with the actual data

- Nonspeech
- × Speech

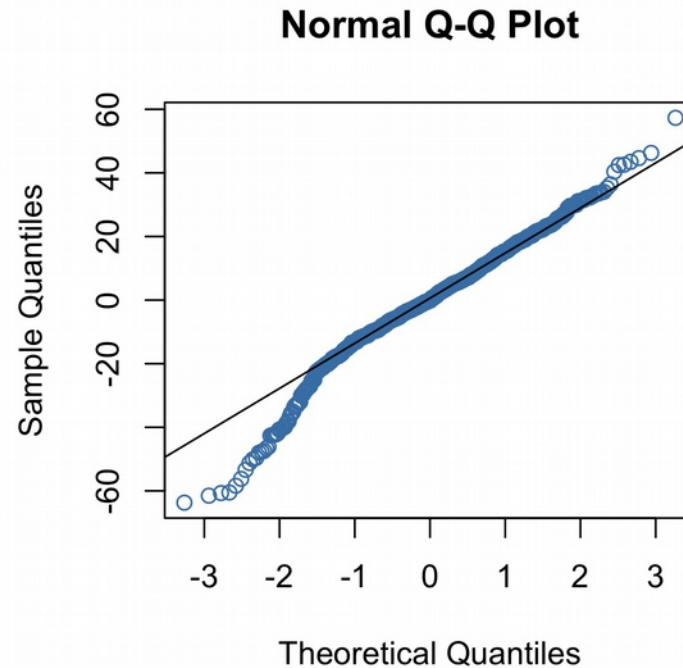
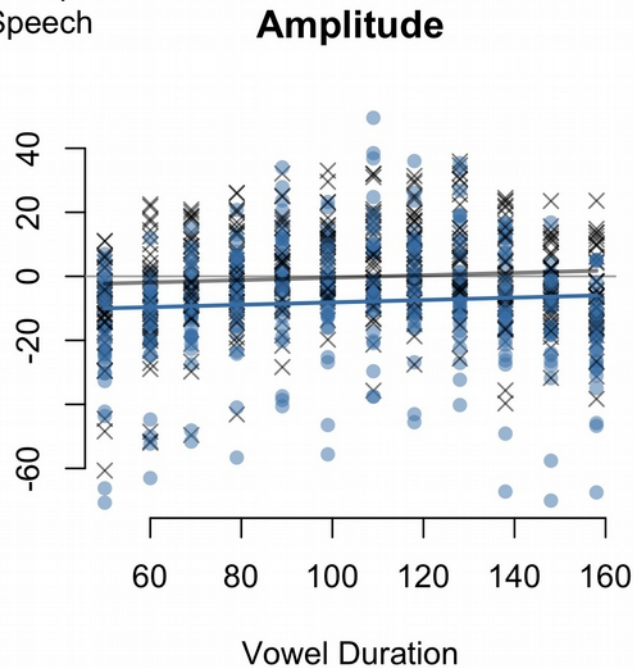




Model criticism

- Inspection of residuals: Comparing the fitted values with the actual data

- Nonspeech
- × Speech





Analyzing time series data using GAMs

Jacolien van Rij & Martijn Wieling | LSA 2015, Chicago
