# LANGUAGE AND INFERENCE

Day 1: Types of Inference Day 2: Designing Meaning Representations Day 3: Building Meaning Representations Day 4: Projection and Presupposition Day 5: Inference in the Real World

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# **Different Logics for Different Needs**



## Logics and how they relate



# Summary of Yesterday

inconsistent «	contradictory true in <b>no</b> models	] )
consistent	<i>synthetic</i> true in <b>some</b> (but not all) models	
	<i>analytic</i> true in <b>all</b> models	<pre> } tautology</pre>

# An example model



M = < D, F > $D=\{d1, d2, d3, d4, d5, d6, d7, d8\}$  $F(man)=\{d1\}$ F(woman)={d2}  $F(house) = \{d3, d4\}$  $F(dog)=\{d5\}$  $F(bird)=\{d6\}$  $F(tree) = \{d7\}$  $F(car) = \{d8\}$  $F(happy)=\{d1,d2\}$  $F(near) = \{(d5, d2), (d2, d5)\}$  $F(at) = \{(d6, d3)\}$ 



**Inference Methods:** 

### Model Building and Theorem Proving

Meaning Representation:

**Design** and **Evaluation** 

# Ways of Inference

- Model Checking
- Model Building (informative, consistent)
- Theorem Proving (non-informative, inconsistent)

# **Model Checking**

• The task of the determining whether a given model satisfies a formula (or a set of formulas)

Input: **model + formula** Output: true or false

# Model Checking

M = < D, F > $D=\{d1, d2, d3, d4\}$ F(mia)=d1 F(honey-bunny)=d2 F(vincent)=d3 F(yolanda)=d4 F(customer)={d1,d3} F(robber)={d2,d4}  $F(love) = \{(d4, d2), (d3, d1)\}$ 

Q1: Does M satisfy:  $\exists x(customer(x) \land \exists y(customer(y) \land love(x,y)))$ Q2: Does M satisfy:  $\exists x(robber(x) \land love(x,x))$ 

 The task of checking whether a formula (or a set of formulas) is satisfiable, or put differently, checking whether there exists a model that satisfies that formula

Input: **formula** Output: **model** (if you're lucky)

 Model building serves to check whether input is consistent and informative!



Q3: Build a model that satisfies:

 $\exists x(robber(x) \land love(x,x))$ 

A robber loves himself

M=<D,F> D={d8} F(robber)={d8} F(love)={(d8,d8)}

Q3: Build a model that satisfies:

 $\exists x(robber(x) \land love(x,x))$ 

A robber loves himself

M=<D,F> D={d7,d8,d9} F(robber)={d8,d9} F(love)={(d7,d8),(d8,d8)}

Q3: Build a model that satisfies:

 $\exists x(robber(x) \land love(x,x))$ 

A robber loves himself



Q4: Build a model that satisfies:

 $\exists x(bkb(x) \land eats(j,x))$ 

Jules eats a big kahuna burger



Q4: Build a model that satisfies:

 $\exists x(bkb(x) \land eats(j,x))$ 

Jules eats a big kahuna burger

$$M =$$
  
 $D = \{d1,....\}$   
 $F(butch) = d1$   
 $F(person) = \{d1,....\}$   
 $F(parent) = \{....\}$ 

Q5: Build a model that satisfies:

person(butch)  $\forall x(person(x) \rightarrow \exists y(person(y) \& parent(x,y)))$   $\forall x \forall y \forall z(parent(x,y) \& parent(y,z) \rightarrow parent(x,z))$  $\neg \exists x parent(x,x)$ 

# Infinitely large models

The following theory (set of formulas) doesn't have a finite model:

```
person(butch)

\forall x(person(x) \rightarrow \exists y(person(y) \& parent(x,y)))

\forall x \forall y \forall z(parent(x,y) \& parent(y,z) \rightarrow parent(x,z))

\neg \exists x parent(x,x)
```

"Everyone has a parent"

## **Theorem Proving**

 The task of checking whether a formula (or a set of formulas) is a validity (a theorem), or put differently, checking whether that formula is true in all models

Input: **formula** Output: **proof** (if you're lucky)

 Theorem proving serves to check whether input is inconsistent and uninformative!

# From Models to Proofs

- Problem with checking whether a formula is a validity (satisfied by all models) is that there are many models...
- Proof theory investigates validity from a purely syntactic perspective (formula manipulation, models play no role)
- Various methods exist we look briefly at just one of them:

# tableaux

### Tableaux

 Refutation proof method: show that F is valid by showing that all attempts to falsify it must fail

$$\begin{array}{c|c|c} \mathbf{f}:A \lor B & \mathbf{t}:A \lor B & \mathbf{f}:A \land B \\ \hline \mathbf{f}:A & \mathbf{t}:A & \mathbf{t}:B & \mathbf{f}:A & \mathbf{f}:B \\ \hline \mathbf{f}:B & \mathbf{t}:A & \mathbf{t}:B & \mathbf{t}:B \\ \hline \mathbf{f}:A \supset B & \mathbf{t}:A \supset B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{t}:B \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{t}:B & \mathbf{t}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{t}:B & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f}:B & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A & \mathbf{f}:A \\ \hline \mathbf{f}:B & \mathbf{f$$

### Combining model building with theorem proving

- We have a method for building models
- We have a method for proving theorems

Let's put these together!

#### **Consistency checking**:

- give F to a model builder; if it finds a model then F consistent
- 2. give ¬F to a theorem prover; it it finds a proof then F inconsistent

### Combining model building with theorem proving

- We have a method for building models
- We have a method for proving theorems

Let's put these together!

#### Informativeness checking:

- give ¬F to a model builder; if it finds a model then F informative
- 2. give F to a theorem prover; it it finds a proof then F uninformative

### The Yin and Yang of Inference



# Theorem Proving and Model Building function as opposite forces

# Good and bad news

(Very) Bad News

- First-order logic is undecidable
- There is no algorithm capable of determining whether an input formula is a theorem or not

(Reasonably) Good News

- First-order logic is actually semi-decidable
- If the input is a theorem, then there is a way to show so (given enough time and memory) – if it's not then all bets are off
- Finding a finite model for a given domain size is decidable

# Moving on...

- What are adequate meaning representations?
- How can we judge whether they are adequate?

# What is an adequate meaning representation formalism?

- 1. Mia smokes  $\rightarrow$  a woman smokes
- 2. Every woman smokes and Mia is a woman  $\rightarrow$  Mia smokes
- 3. A tall woman smokes  $\rightarrow$  a woman smokes
- 4. Mia smokes silently  $\rightarrow$  Mia smokes
- 5. Mia smokes a cigarette  $\rightarrow$  Mia smokes
- 6. Mia smokes a cigarette at a table  $\rightarrow$  Mia smokes at a table
- 7. Mia smiles and smokes  $\rightarrow$  Mia smiles
- 8. Mia met Vincent → Vincent met Mia
- 9. Mia is taller than Vincent  $\rightarrow$  Vincent is not taller than Mia.
- 10. Mia is the tallest woman  $\rightarrow$  Mia is taller than Yolanda.
- 11. Mia is taller than Vincent and Vincent is tall  $\rightarrow$  Mia is tall.
- 12. Vincent saw a woman. She smokes.  $\rightarrow$  a woman smokes.

## Case Study 1: .....

#### Translation

Background Knowledge (aka Meaning Postulates)

Translation

Mia smokes: p121

A woman smokes: p247

Background Knowledge

p121 → p247

- silly: doesn't scale
- need a new propositional variable for every sentence

Translation

Mia smokes: mia(smokes)

A woman smokes: a-woman(smokes)

Background Knowledge

 $\forall x(mia(x) \rightarrow a-woman(x))$ 

- bad choice predicate/argument
- doesn't scale to transitive verbs

Translation

Mia smokes: smokes(mia)

A woman smokes: smokes(a-woman)

Background Knowledge

∀x(x=mia→x=a-woman)

- better predicate/argument choice
- noun phrases don't scale
- need a different constant for each noun phrase (silly)

	Translation	
Mia smokes:		smokes(mia)
A woman smokes:		∃x(woman(x)∧smokes(x))
	Background Knowledge	
woman(mia)		
	Critical Reflection	
- this is promising		

# Case Study 2: Every woman smokes and Mia is a woman $\rightarrow$ Mia smokes

Translation

Every woman smokes:	∃x(woman(x)∧smokes(x))
Mia is a woman:	woman(mia)
Mia smokes:	smokes(mia)

Background Knowledge

- wrong choice of quantifier
- required entailment not produced

# Case Study 2: Every woman smokes and Mia is a woman $\rightarrow$ Mia smokes

Translation

Every woman smokes:	∀x(woman(x)∧smokes(x))
Mia is a woman:	woman(mia)
Mia smokes:	smokes(mia)

Background Knowledge

- better choice of quantifier
- we get the inference
- but true only in a female smoky worlds

# Case Study 2: Every woman smokes and Mia is a woman $\rightarrow$ Mia smokes

Translation

Every woman smokes:	$\forall x(woman(x) \rightarrow smokes(x))$
Mia is a woman:	woman(mia)
Mia smokes:	smokes(mia)

Background Knowledge

- we get the inference
- proper restriction of the universal quantifier

### Case Study 3: A tall woman smokes $\rightarrow$ a woman smokes

Translation

A tall woman smokes:∃x(tall-woman(x)∧smokes(x))A woman smokes:∃x(woman(x)∧smokes(x))

Background Knowledge

 $\forall x(tall-woman(x) \rightarrow woman(x))$ 

- doesn't scale
- need a lot of BK rules for all adjective-noun combinations

### Case Study 3: A tall woman smokes → a woman smokes

Translation

A tall woman smokes:∃x(tall(x)∧woman(x)∧smokes(x))A woman smokes:∃x(woman(x)∧smokes(x))

Background Knowledge

- scales
- no BK rules needed
- works for intersective adjectives, but not for subsective ones

### Case Study 4: Mia smokes silently $\rightarrow$ Mia smokes

Translation

Mia smokes silently:smokes-silently(mia)Mia smokes:smokes(mia)

Background Knowledge

 $\forall x(\text{smokes-silently}(x) \rightarrow \text{smokes}(x))$ 

- doesn't scale
- need a lot of BK rules for all adverbverb combinations
- but what do we do?

### Case Study 4: Mia smokes silently $\rightarrow$ Mia smokes

Translation

Mia smokes silently: $\exists x(smokes(x,mia) \land silently(x))$ Mia smokes: $\exists x smokes(x,mia)$ 

Background Knowledge

- scales
- no BK needed
- known as Davidsonian analysis

### Case Study 5: Mia smokes a cigarette $\rightarrow$ Mia smokes

Translation

Mia smokes a cigarette:  $\exists x(cigarette(x) \land \exists y smokes(y,mia,x))$ Mia smokes: $\exists x smokes(x,mia)$ 

Background Knowledge

 $\forall x \forall y \forall z (smokes(x,y,z) \rightarrow smokes(x,y))$ 

- looking promising
- but BK needed to model optional arguments
- alternatives?

# **Thematic Roles**

- Roles of all participants in an event
- The who does what to whom, where and when
- Example role inventory (subset of VerbNet):

agent: human or animate volitional participant patient: participant undergoing a process theme: participant undergoing a change of location location: spatial location experiencer: participant that is experiencing something instrument: objects that come into contact with an object

and cause some change in them

### Case Study 5: Mia smokes a cigarette $\rightarrow$ Mia smokes

Translation

Mia smokes a cigarette:

∃e∃x(cigarette(x)^smokes(e)^agent(e,mia)^patient(e,x))

#### Mia smokes:

∃e(smokes(e)∧agent(e,mia))

Background Knowledge

- no BK required
- instead new inventory of thematic roles
- known as *neo-Davidsonian* analysis



Mia smokes a cigarette at a table → Mia smokes at a table

Translation

Mia smokes a cigarette at a table:

∃e∃x∃y(cigarette(x)^smokes(e)^agent(e,mia)^patient(e,x)^at(e,y)^table(y))

Mia smokes at a table:

∃e∃x(smokes(e)∧agent(e,mia)∧at(e,x)∧table(x))

Background Knowledge

- no BK required
- neo-Davidsonian approach naturally extends to other verb modifiers

### Case Study 7: Mia smiles and smokes $\rightarrow$ Mia smiles

Translation

Mia smiles and smokes: $\exists e(smiles-and-smokes(e) \land agent(e,mia))$ Mia smiles: $\exists e(smiles(e) \land agent(e,mia))$ 

Background Knowledge

 $\forall x(smiles-and-smokes(x) \rightarrow smokes(x))$ 

 $\forall x (smokes-and-smiles(x) \rightarrow smokes(x))$ 

- silly again...
- make use of boolean connectives

### Case Study 7: Mia smiles and smokes $\rightarrow$ Mia smiles

Translation

#### Mia smiles and smokes:

∃e∃e'(smiles(e)∧agent(e,mia)∧smokes(e')∧agent(e',mia))

**Mia smiles**: ∃e(smiles(e)∧agent(e,mia))

Background Knowledge

**Critical Reflection** 

- much better

### Case Study 8: Mia met Vincent → Vincent met Mia

Translation

**Mia met Vincent**:  $\exists e(meet(e) \land agent(e,mia) \land co-agent(e,vincent))$ **Vincent met Mia**:  $\exists e(meet(e) \land agent(e,vincent) \land co-agent(e,mia))$ 

Background Knowledge

 $\forall e \forall x (meet(e) \land agent(e, x) \rightarrow co-agent(e, x))$ 

 $\forall e \forall x (meet(e) \land co-agent(e, x) \rightarrow agent(e, x))$ 

**Critical Reflection** 

- can we do without BK?

# Case Study 9: Mia is taller than Vincent $\rightarrow$ Vincent is not taller than Mia.

Translation

Mia is taller than Vincent:

∃e(be-taller(e)∧theme(e,mia)∧than(e,vincent))

Vincent is not taller than Vincent:

¬∃e(be-taller(e)∧theme(e,vincent)∧than(e,mia))

Background Knowledge

 $\forall e \forall x \forall y (be-taller(e) \land theme(e,x) \land than(e,y) \rightarrow taller(x,y))$ 

```
\forall x \forall y \forall z((taller(x,y) \land taller(y,z)) \rightarrow taller(x,z))
```

¬∃x taller(x,x)

**Critical Reflection** 

- can we do without BK?

## Case Study 10:

Mia is the tallest woman → Mia is taller than Yolanda

Translation

Mia is the tallest woman:

∃e(be-tallest(e)∧theme(e,mia)∧woman(mia))

#### Mia is taller than Yolanda:

∃e(be-taller(e)∧theme(e,mia)∧than(e,yolanda))

Background Knowledge

 $\forall e \forall x (be-tallest(e) \land theme(e,x)) \rightarrow \forall y (\neg x = y \rightarrow taller(x,y))$ 

 $\forall e \forall x \forall y ((be-taller(e) \land theme(e,x) \land than(e,y)) \rightarrow taller(x,y))$ 

```
\forall x \forall y \forall y ((taller(x,y) \land taller(y,z)) \rightarrow taller(x,z))
```

¬∃x taller(x,x)

**Critical Reflection** 

- restriction

# **Powerful but Limited**

Many things that we haven't considered can be modeled or approximated with firstorder logic

- modalities
- plurals
- tense and aspect

However, several natural language phenomena can't be handled by first-order logic

- relational quantifiers: most, few, many
- cardinal expressions (clumsy in FOL)
- intersective adjectives

generics

# Moving from sentences to text

- First-order Logic
- Discourse Representation Theory (DRT)

# **Discourse Representation Theory**

- DRT is a formal semantic theory of text
- Predicts difference in acceptability of pronouns
- It employs box-like representations (DRS)